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PROTOTIPADO BRAZO ROBÓTICO SOLDADURA

WELDING ROBOTIC ARM PROTOTYPE

Quito-2026

# CERTIFICATE OF AUTHORSHIP

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## **APROBACIÓN DEL TUTOR**

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**DIRECTOR DEL TRABAJO DE TITULACIÓN**

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## Chapter 1

### INTRODUCTION

Technological evolution has fundamentally transformed industrial environments, driving the transition towards Industry 4.0. This paradigm shift prioritizes not only production efficiency and cost reduction but also the maximization of product quality and safety. Within this context, robotic manipulators have emerged as indispensable tools, capable of replicating and often surpassing human dexterity in repetitive or high-precision tasks across sectors such as manufacturing, medicine, and research [1, 2].

Specifically in the field of metalworking, arc welding is a critical process that demands strict adherence to technical standards. Regulations such as the AWS D1.1 code, established by the American Welding Society [3], define precise guidelines for structural steel welding. Achieving compliance with such rigorous standards through manual operation is increasingly challenging due to human fatigue and variability. Consequently, automation through robotics becomes essential to maintain the consistent parameters—such as speed and trajectory—mandated by these regulations.

To address these challenges, Six-degree-of-freedom (6-DOF) robotic arms represent a significant technological solution. By providing a three-dimensional workspace with complex rotations and transitions, they simulate the kinematics of a human arm, making them ideal for executing intricate welding trajectories such as circular or linear paths with high repeatability [4, 5]. However, the implementation of such technology presents operational challenges for Small and Medium-sized Enterprises (SMEs), which often lack the capital to invest in physical robotic infrastructure. This financial limitation hinders their ability to perform precise trajectory analysis and production optimization.

To bridge this gap, and in collaboration with the company CNESTRONIC, this project focuses on developing a high-fidelity virtual prototype of a 6-DOF robotic arm with a workspace of approximately  $1 \text{ m}^3$ , specifically engineered for welding applications. A critical aspect of this proposal is the adherence to recognized industrial parameters. The system is designed to validate specific welding requirements, such as a continuous

welding dimension of 3.2 mm (equivalent to 1/8 inch standards) and an intermittent welding spacing of 40 mm. These values, based on technical infrastructure norms [6] and aligned with standards like AWS D1.1 [3], serve as a benchmark to guarantee the feasibility of the welding process before any physical implementation, significantly reducing development risks [7].

Therefore, the project adopts an exclusively virtual phase utilizing SolidWorks and MATLAB to model, simulate, and validate kinematic behavior. This methodology serves a dual purpose: it supports the technical validation supported by recent simulation studies [8, 9], and fulfills a vital educational role by training mechatronic engineers in complex areas such as inverse kinematics and trajectory control within a safe environment [10]. Ultimately, this establishes a robust foundation for future physical implementations, integrating improvements such as artificial intelligence algorithms for trajectory optimization.

Based on the identified needs and the proposed technological solution, the general objective of this project is to develop a robotic arm capable of performing welding tasks automatically, accurately, and safely through simulation.

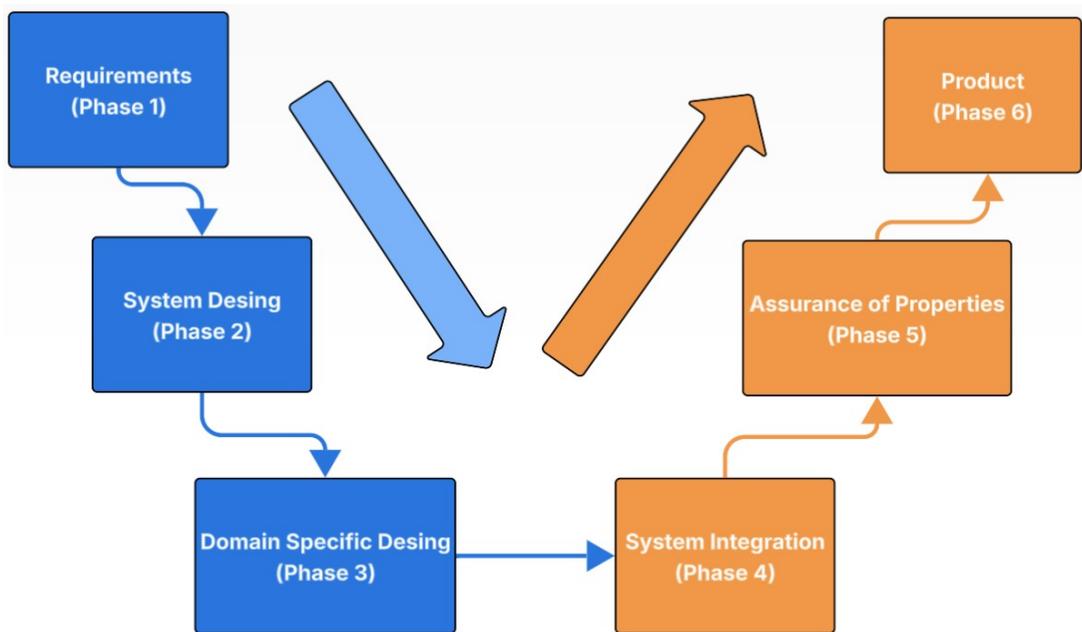
To fulfill the general objective, the following specific goals have been proposed:

- Design a robotic arm capable of performing welding tasks, considering its structure, components, and control system.
- Develop forward and inverse kinematic models of the robotic arm to precisely control its movements within the simulation environment.
- Validate the operation of the simulated model through virtual testing to evaluate its accuracy and performance.

## Chapter 2

### METHODOLOGY AND DESIGN

The design of the robotic arm followed the VDI 2206 methodology. This framework organizes the development into seven sequential phases, ensuring a structured progression from requirements definition to virtual validation, as shown in Figure 1.



**Figure 1.** Project workflow based on the VDI 2206 V-Model.

As detailed in Figure 1, the workflow is organized into a continuous stream divided into three main stages. The descending branch (Phases 1–3) focuses on the definition and design of the system, translating high-level requirements such as a  $1\text{ m}^3$  workspace and a 5 kg payload into a specific anthropomorphic configuration and the detailed selection of mechanical and electrical components. The vertex of the "V" represents the core implementation stage, where mathematical modeling and kinematic analysis are executed within the MATLAB environment. Finally, the ascending branch (Phases 4–6) addresses the virtual verification of the system, starting with kinematic integration and path planning, followed by rigorous property assurance to ensure torque limits remain below 450 Nm, and culminating in the delivery of a fully validated virtual prototype optimized for automated MIG welding tasks.

## **2.1. STAGE I: SYSTEM DEFINITION AND DESIGN**

### **2.1.1. Application of the VDI 2206 Methodology**

After defining the project, the VDI 2206 methodology was selected as the framework for designing the 6-DOF robotic arm for MIG welding. This methodology structures the development and defines the key system requirements:

#### **1. Functional Requirements**

- Follow planned trajectories accurately.
- Move smoothly during continuous operation.
- Move from one position to another in point-to-point mode.
- Perform automated welding tasks.

#### **2. Non-Functional Requirements**

- The trajectories to be followed are a square, a circle, and a linear path along the z-axis.
- The robotic arm must be designed to support a payload of at least 5 kg at the end effector.
- The system must maintain a constant linear velocity at the end effector during trajectory execution.
- The system must be modular to allow for quick changes without having to break or rebuild the entire robot.

#### **3. Design Constraints**

- The manipulator must have six degrees of freedom (6-DOF) to reach the required positions and orientations within the workspace.
- Limitations in materials for the prototype, considering the use of ABS and aluminum.
- Maximum working reach is defined as 1 m<sup>3</sup>.

- Development is limited to a virtual prototype during this phase, without physical construction.
- Exclusive use of free or educational software platforms (MATLAB/Simulink, SolidWorks Student, Fusion 360).

### 2.1.2. System Requirements Definition

The development of this project is based on the preliminary requirements, which allow for the simulation of a 6-degree-of-freedom robotic arm. The following requirements are presented:

- The robotic arm must reach a size of 1 m<sup>3</sup> in accordance with CNESTRONIC's specifications.
- The robotic arm must have six degrees of freedom to perform tasks remotely, with the aim of reducing workers' exposure to hazardous environments.
- This project must be carried out in simulation.

### 2.1.3. Architectures according to the VDI 2206 methodology

#### 1. Functional Architecture:

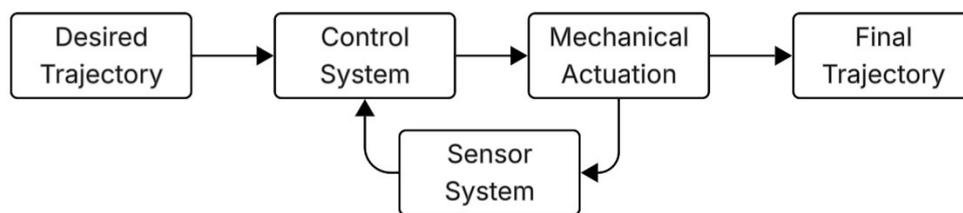
This stage defined the functional architecture required for the effective operation of the robotic arm. The process begins with the input of the desired trajectory, which is processed by the control center to drive the actuators. Subsequently, through the application of forward and inverse kinematics, the physical output trajectory is executed based on the initial configuration parameters. These functions work synergistically to ensure precision, repeatability, and safety during the welding process, as illustrated in Figure 2.



**Figure 2.** Functional architecture of the 6 dof.

## 2. Logical Architecture:

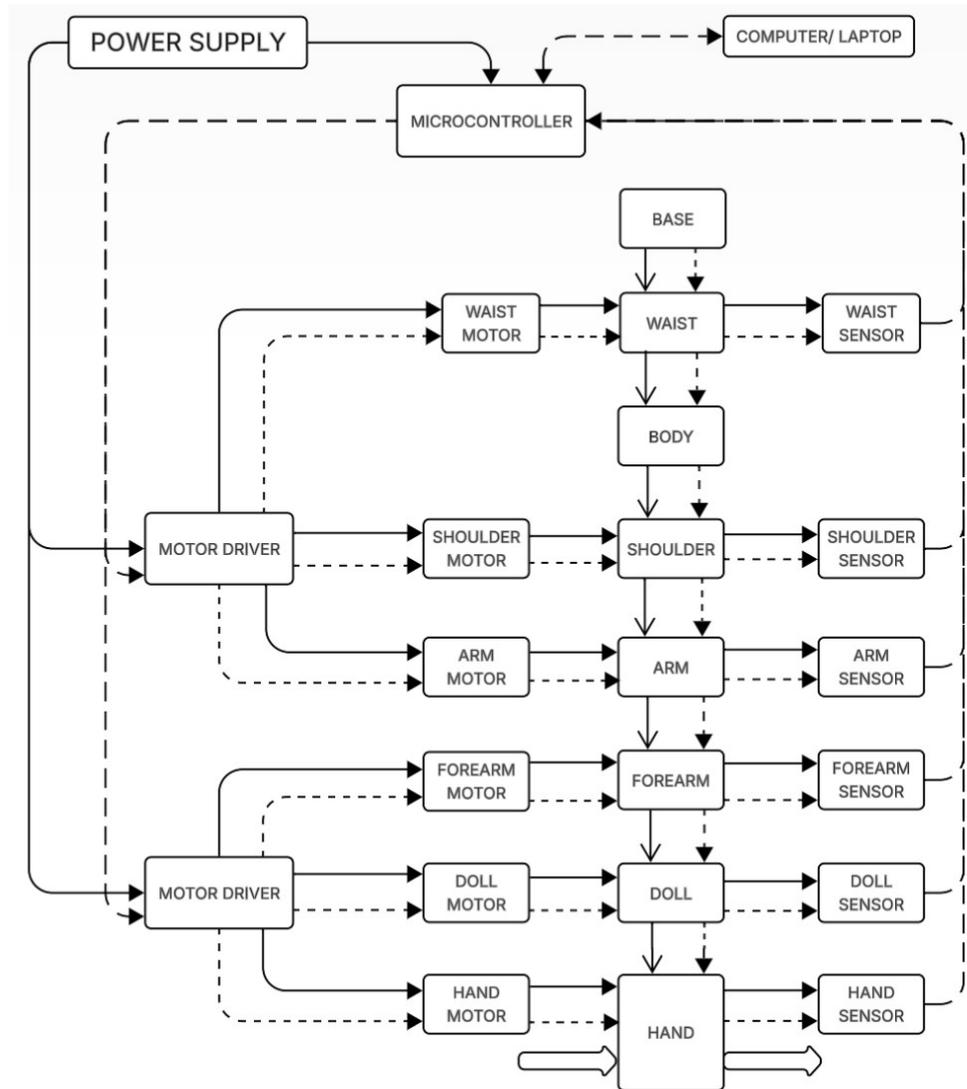
This stage defines the information exchange protocol between the robotic arm subsystems. The operation begins with the transmission of the desired trajectory, prompting the control system to execute the necessary kinematic calculations to drive the mechanical actuation. Simultaneously, the sensor system detects the actual motion and provides feedback to the control system, which adjusts the parameters to ensure the output aligns with the desired final trajectory. The corresponding logical architecture is shown in Figure 3.



**Figure 3.** Logical architecture of the 6 dof.

## 3. Physical Architecture:

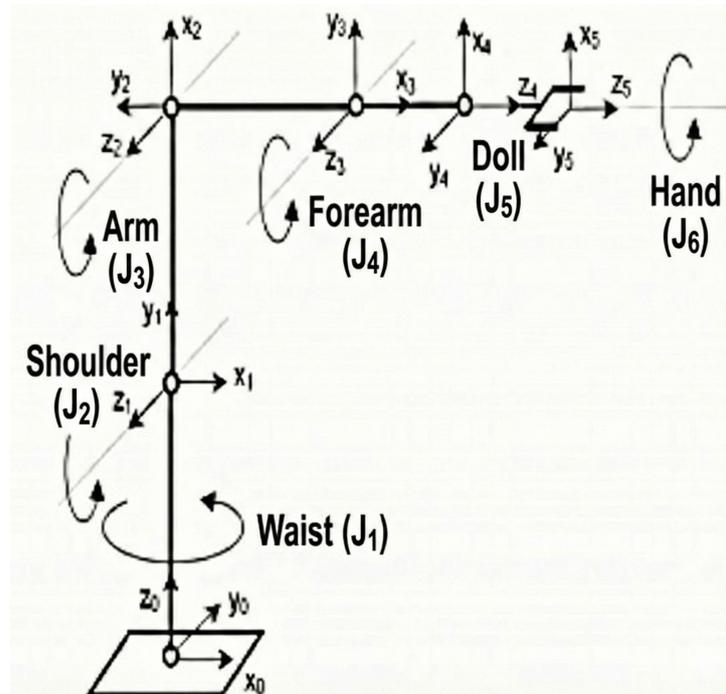
The robotic arm in this architecture is based on the specific organization of the elements that will be used if implemented, where the power supply provides energy to both the microcontroller and the drivers responsible for activating the motors distributed in each joint involved, which are “waist, shoulder, arm, forearm, doll, and hand.” The microcontroller receives instructions from the computer running the code, sends control signals to the drivers, and receives feedback from the sensors associated with each motor, allowing for closed-loop control of position and movement. Although the system is developed in a simulation environment, a structural representation equivalent to that of a real robotic arm is established for each link and joint. The integration of these elements within the simulation platform allows for the analysis of kinematic behavior, verification of trajectories, and validation of control strategies without requiring physical hardware, as shown in Figure 4.



**Figure 4.** Physical architecture of the 6 dof.

#### 2.1.4. Conceptual Manipulator Design

The proposed manipulator is based on a 6-degree-of-freedom (6-DOF) configuration, chosen for its versatility in welding [7] and adaptability to manageable scales [11, 12]. Given the high costs of industrial equipment, the literature supports the design of modular and accessible educational prototypes [1, 10, 13–16]. To illustrate this motion architecture, Figure 5 presents the theoretical kinematic diagram alongside its implementation in the simulation environment, visualizing the physical correspondence of each joint.



**Figure 5.** Kinematic diagram and simulation model of the 6-DOF arm [17].

Based on the anthropomorphic architecture detailed in Figure 5, the system consists of a serial kinematic chain composed of rotational joints and rigid links [17]. The main components are described below:

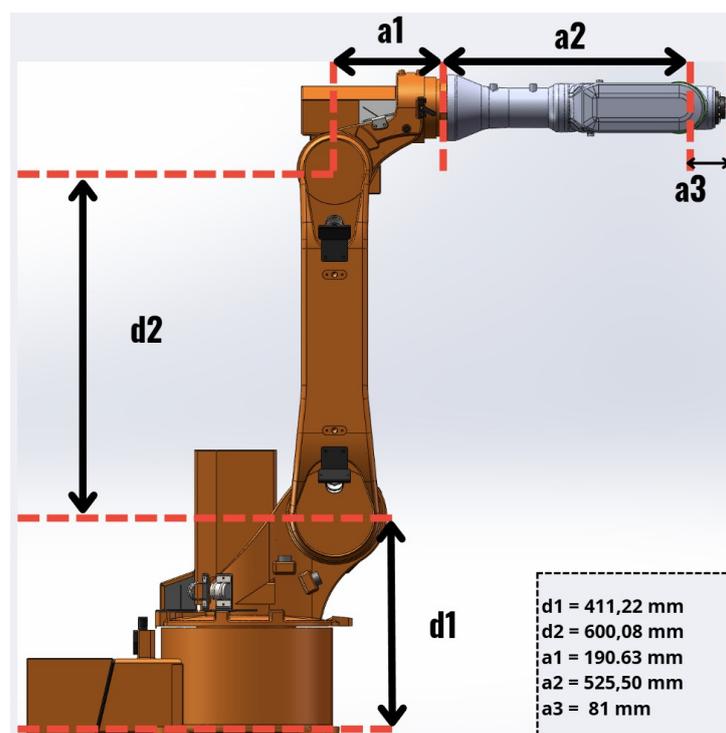
- **Joints:** The robot features 6 rotational joints ( $J_1$  to  $J_6$ ) that define its degrees of freedom:
  1. **Waist ( $J_1$ ):** Allows rotation of the base around the vertical axis ( $z_0$ ), defining the robot's azimuthal positioning.
  2. **Shoulder ( $J_2$ ):** The joint responsible for the main lifting of the arm, acting on the horizontal axis ( $z_1$ ).
  3. **Elbow ( $J_3$ ):** Provides extension and flexion of the arm, complementing the vertical and radial reach.
  4. **Forearm ( $J_4$ ):** Enables longitudinal rotation of the forearm, which is crucial for tool orientation.
  5. **Doll ( $J_5$ ):** The joint responsible for the pitch motion of the end tool.
  6. **Hand ( $J_6$ ):** Performs the final roll rotation to orient the end-effector in the welding direction.

- **Links:** Rigid elements that connect the joints and determine the robot's workspace volume. Key links include the base link, the arm link (between  $J_2$  and  $J_3$ ), and the forearm link (between  $J_3$  and the wrist).
- **End-Effector:** Located after joint  $J_6$ , this is the mounting point for the MIG welding torch. Its position and orientation (Pose) are the result of the vector sum of all preceding movements.

## 2.2. STAGE II: VIRTUAL IMPLEMENTATION AND MODELING

### 2.2.1. Specific Design

Considering the kinematic and dynamic constraints imposed by critical welding parameters (speed, angle, and stick-out), the design was developed to maximize precision. For the development of the model in a virtual environment, the **ESTUN AUTOMATION ER20-1780-F industrial robot** is taken as a reference. This 6-DOF manipulator features a 16 kg payload capacity, a maximum reach of 1780 mm, and a repeatability of 0.1 mm, geometric characteristics detailed in Figure 6 that ensure the stability required for the process.



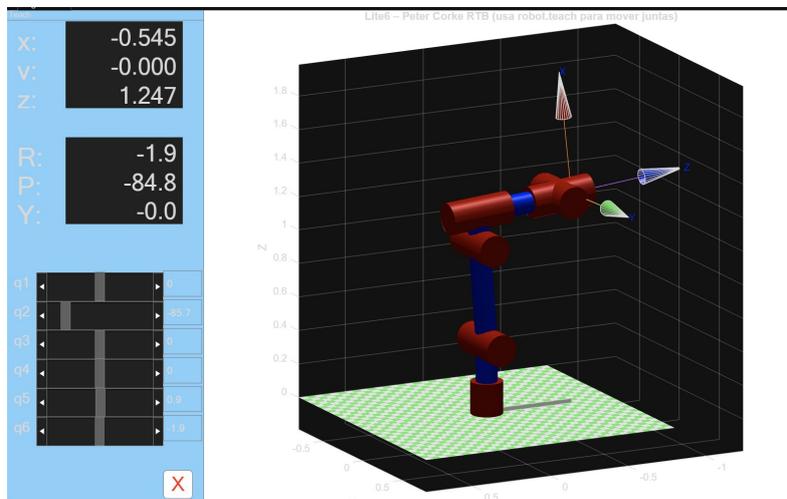
**Figure 6.** Dimensional Parameters of the Articulated Manipulator.

Based on this architecture, geometric modeling is performed in MATLAB using the Robotics Toolbox, a standard practice in research for manipulator simulation and validation [4, 5, 9, 18–21]. To define the system kinematics, the Denavit-Hartenberg (DH) parameters [22] are employed to establish the transformations between joints, as presented in Table 1.

**Table 1.** Denavit-Hartenberg Parameters of the 6-DOF Robotic Arm

Joint	$a_i$ (m)	$\alpha_i$ (rad)	$d_i$ (m)	$\theta_i$ (rad)
1	0	$-\frac{\pi}{2}$	$d1$	0
2	$d2$	0	0	0
3	$a1$	$\frac{\pi}{2}$	0	0
4	0	$-\frac{\pi}{2}$	$a2$	0
5	0	$\frac{\pi}{2}$	0	0
6	0	0	$a3$	0

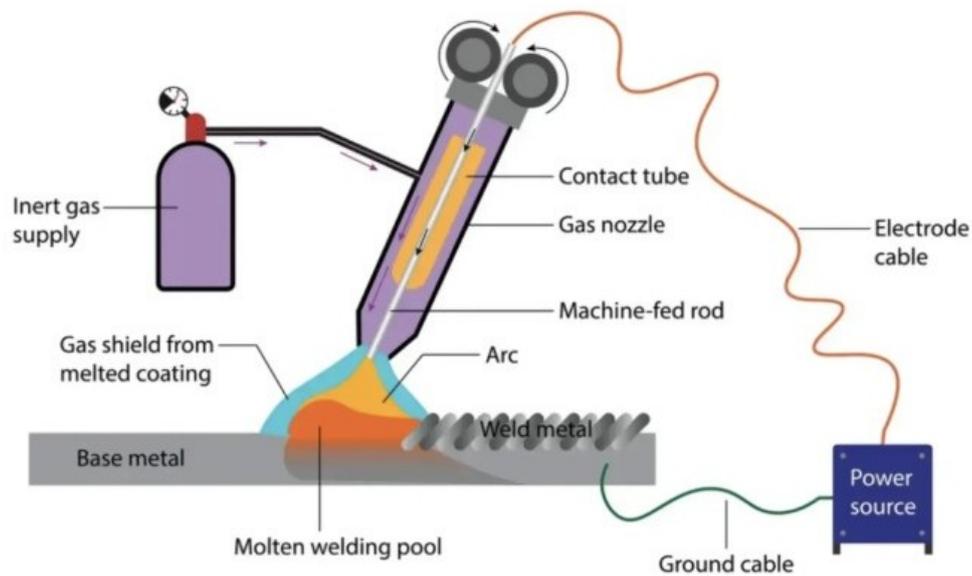
Furthermore, utilizing the tools provided by the Robotics Toolbox (RTB) for MATLAB, developed by Peter Corke [23], it was possible to model and visualize the kinematic structure of the robotic arm using the defined Denavit-Hartenberg parameters. This toolbox enabled the individual manipulation of each joint, verifying that the generated movements were consistent with the established geometric configuration. The resulting visualization confirms the correct kinematic behavior of the manipulator, as shown in Figure 7. This validation allowed for the identification of the HOME point, which serves as the initial reference for executing the trajectories developed in this project.



**Figure 7.** Control and Position View for a 6-DOF Robot using RTB.

### 2.2.1.1. Robotics and Welding Automation

Welding automation is crucial in industrial robotics for ensuring precision and safety. In the literature, [24] and [15] address kinematics and design for specific applications. To meet rigorous quality standards, [8] optimizes parameters through simulation, while [2] integrates machine vision for real-time trajectory control. In this context, Figure 8 illustrates the essential physical components of the MIG process required for proper execution [25].



**Figure 8.** Structure and main components of the MIG welding process [25].

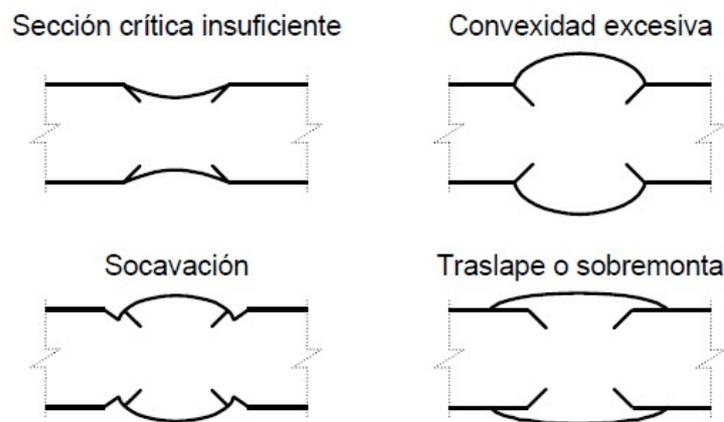
It also highlights the elements directly involved in the formation of the arc and in the protection of the molten pool, emphasizing the latter as the region of metal that remains in a liquid state under the action of the electric arc and which, with adequate gas protection, subsequently solidifies to form a stable, contamination-free bead.

### 2.2.1.2. Focus on Gas Metal Arc Welding (GMAW - MIG)

Among automation techniques, Gas Metal Arc Welding (GMAW), commercially known as MIG, holds a prominent position. This method utilizes a continuously fed wire electrode through a torch, alongside an inert or active shielding gas flow (argon, CO<sub>2</sub>, or mixtures) to protect the weld pool from atmospheric contamination. Due to the nature of the process, its robotic implementation demands millimeter precision. As indicated by [1] and [8], geometric validation is a determinant of final quality; consequently, en-

uring operational stability and achieving defect-free beads necessitates the rigorous management of the following critical parameters:

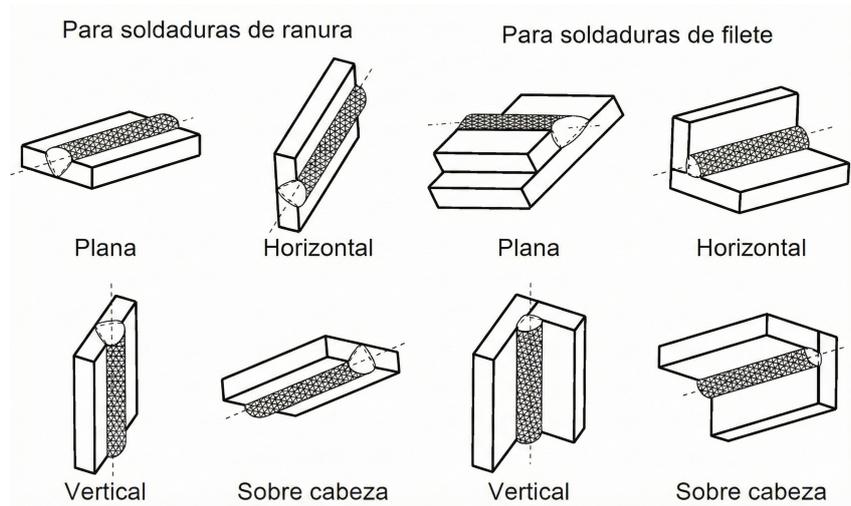
- **TRAVEL SPEED:** This is the rate at which the robot moves the torch, and it is the most critical factor as it directly dictates the heat input to the metal [4]. In industrial MIG processes, this speed typically ranges between 6 and 12 mm/s (350 to 750 mm/min). Incorrect control of this parameter leads to the defects illustrated in the Figure 9.



**Figure 9.** Defective profiles in groove welding on butt joints [6].

As shown in the figure, travel speed deviations cause structural failures: excessive speed results in incomplete fusion due to low heat input, while slow speed causes excessive convexity and undercutting. Since these defects contravene the technical fundamentals described in [6] and are direct grounds for rejection under the AWS D1.1 standard [3], operating within the established range is mandatory. To ensure this compliance, thermal simulation [8] and real-time correction algorithms [2] are essential for maintaining constant speed.

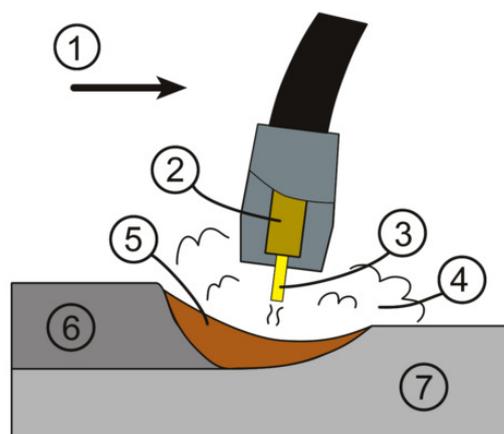
- **TORCH ANGLE:** This is a critical parameter that directly controls heat distribution, penetration, and bead morphology [1]. In robotic MIG welding, it is essential that the torch maintain a precise angle, typically between  $0^\circ$  and  $15^\circ$  relative to the perpendicular of the bead. Deviation from this range negatively impacts the uniformity of the molten pool and can cause spatter. The different types of spatter can be seen in the Figure 10.



**Figure 10.** Positions for performing welding [6].

Given that this study will focus primarily on the Flat and Vertical welding positions, the robot's ability to maintain this precise angle will be tested under different gravitational forces. This capability represents a fundamental challenge in kinematic design, as it demands rigorous validation of its Inverse Kinematics to ensure accessibility to all welding points, even in complex geometries, as emphasized by studies such as [3, 6, 24].

- **STICK-OUT:** Defined as the wire extension beyond the contact tip, this parameter governs electrical resistance and welding current. According to [15], excessive length reduces penetration, while a short length risks overheating. Maintaining this distance requires high structural rigidity and precision, alongside dynamic control algorithms capable of compensating for geometric irregularities [4, 26].



**Figure 11.** Positions for performing welding [26].

As illustrated in Figure 11, the welding operation proceeds along the **Direction of travel (1)**, where the stick-out is defined by the extension of the **Electrode (3)** exiting the **Contact tube (2)** towards the **Workpiece (7)**. While the **Shielding gas (4)** protects the arc environment, maintaining the correct stick-out distance is critical for thermal stability. A deviation causing an excessively long stick-out reduces the welding current, preventing the **Molten weld metal (5)** from reaching the necessary temperature to properly fuse with the base material [26]. This results in defects within the final **Solidified weld metal (6)**, specifically Incomplete Fusion. According to the standard [6], “there shall be complete fusion between the filler metal and the base metal”. Any joint failing to meet this requirement due to inconsistent electrode extension must be rejected. Therefore, achieving fusion completeness is mandatory, making trajectory validation indispensable.

## 2.2.2. Mathematical and Kinematic Modeling

This section presents the complete mathematical framework used in the project, including the forward kinematics for obtaining the end-effector pose and the inverse kinematics for computing the joint angles required to achieve a desired pose. The model is based on the Denavit–Hartenberg parameters listed in Table 1.

### 2.2.2.1. Forward Kinematics

The homogeneous transformation between frames  $i - 1$  and  $i$  using the standard DH convention is:

$$A_i \equiv {}^{i-1}T_i = \begin{pmatrix} \cos \theta_i & -\sin \theta_i \cos \alpha_i & \sin \theta_i \sin \alpha_i & a_i \cos \theta_i \\ \sin \theta_i & \cos \theta_i \cos \alpha_i & -\cos \theta_i \sin \alpha_i & a_i \sin \theta_i \\ 0 & \sin \alpha_i & \cos \alpha_i & d_i \\ 0 & 0 & 0 & 1 \end{pmatrix}.$$

For a 6-DOF manipulator, the matrices  $A_1, \dots, A_6$  are multiplied sequentially to obtain

the full transformation from the base to the end-effector:

$$T \equiv {}^0T_6 = A_1 A_2 A_3 A_4 A_5 A_6 = \begin{pmatrix} R & p \\ \mathbf{0}_{1 \times 3} & 1 \end{pmatrix},$$

where  $R \in R^{3 \times 3}$  is the rotation matrix and  $p \in R^3$  is the end-effector position. Using the joint vector  $\theta = [\theta_1, \dots, \theta_6]$ , the forward kinematics function is:

$$T(\theta) = A_1(\theta_1) A_2(\theta_2) \cdots A_6(\theta_6).$$

### 2.2.2.2. Geometric Parameters and Home Position

The geometric parameters used in the model are:

$$\begin{aligned} d_1 &= 0.41122 \text{ m}, & d_2 &= 0.60008 \text{ m}, & a_1 &= 0.19063 \text{ m}, \\ a_2 &= 0.52550 \text{ m}, & a_3 &= 0.08100 \text{ m}, \end{aligned}$$

with twist angles:

$$\alpha_1 = -\frac{\pi}{2}, \quad \alpha_2 = 0, \quad \alpha_3 = \frac{\pi}{2}, \quad \alpha_4 = -\frac{\pi}{2}, \quad \alpha_5 = \frac{\pi}{2}, \quad \alpha_6 = 0.$$

In the *Home* configuration ( $\theta_i = 0$ ), the end-effector position is:

$$\mathbf{P}_{\text{Home}} = \begin{pmatrix} 0 \\ -(L_2 + L_3 + L_5) \\ L_1 + L_4 \end{pmatrix},$$

With numeric values:

$$\begin{aligned} L_1 &= 0.41122 \text{ m}, & L_2 &= 0.60008 \text{ m}, & L_3 &= 0.19063 \text{ m}, \\ L_4 &= 0.52550 \text{ m}, & L_5 &= 0.08100 \text{ m}. \end{aligned}$$

Thus,

$$\mathbf{P}_{\text{Home}} = \begin{pmatrix} 0 \\ -0.87171 \\ 0.93672 \end{pmatrix} \text{ m.}$$

This matrix represents the initial rest position, which serves as the starting point for all control trajectories, as can be clearly seen in Figure 6.

### 2.2.2.3. Jacobian and Singularities

The geometric Jacobian is:

$$J(\mathbf{q}) = \begin{pmatrix} J_v(\mathbf{q}) \\ J_\omega(\mathbf{q}) \end{pmatrix},$$

with

$$J_v^{(i)} = z_{i-1} \times (p_6 - p_{i-1}), \quad J_\omega^{(i)} = z_{i-1}.$$

Singular configurations occur when the Jacobian loses rank, typically when its determinant or singular values approach zero. These configurations reduce manipulability and must be avoided during trajectory planning.

### 2.2.3. Programming and Control Implementation

To develop the code base used to generate and simulate the movements of the robotic arm, a structured approach was implemented, divided into two main stages: trajectory generation in MATLAB and dynamic control validation in Simulink.

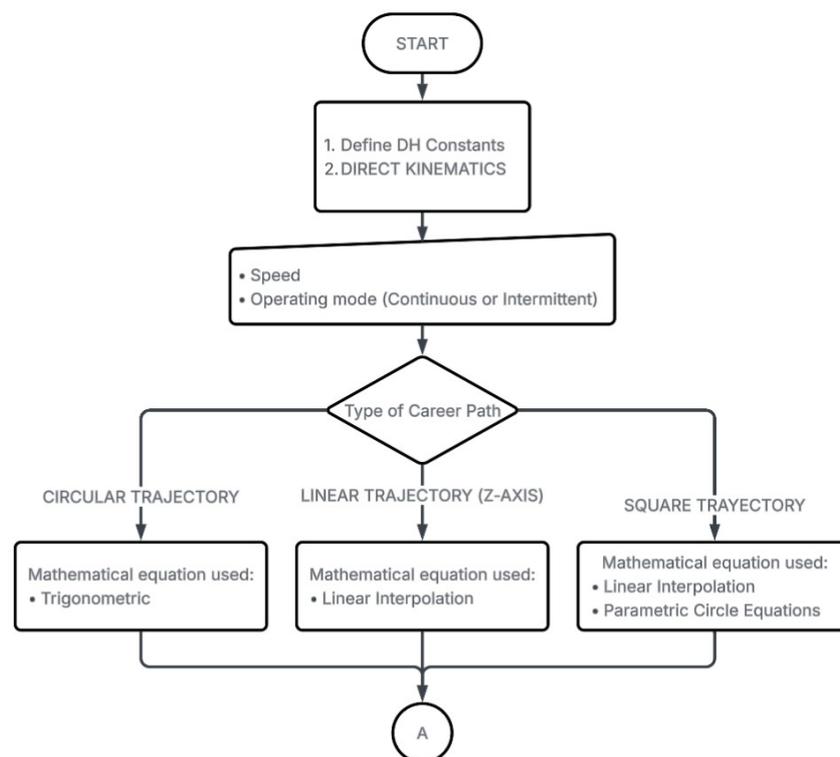
#### 2.2.3.1. Trajectory Generation and Kinematic Algorithms

The computational routine developed for this project generates precise movement commands based on the robot's kinematic model. The complete logic is structured into a unified flowchart, divided for clarity into two main stages: System Configuration and Motion Execution.

The initialization phase, illustrated in Figure 12, begins by defining the geometric constants and Denavit–Hartenberg (DH) parameters required to construct the robot's morphology and compute the **Direct Kinematics**. Subsequently, the system establishes

the operational parameters, specifically the **Speed** and the **Operating Mode** (Continuous or Intermittent). Based on the selected **Type of Career Path**, the algorithm branches into three specific motion profiles, each governed by a distinct mathematical formulation:

- **Linear Trajectory (Z-Axis):** Generated using **Linear Interpolation** equations to produce vertical displacement.
- **Circular Trajectory:** Calculated using **Trigonometric** parametric equations ( $R \cos \theta, R \sin \theta$ ) to maintain a constant radius.
- **Square Trajectory:** Constructed using a hybrid approach where straight segments utilize **Linear Interpolation**, while corners employ **Parametric Circle Equations** for smooth blending.



**Figure 12.** Flowchart Part 1: System Initialization and Geometric Trajectory Selection.

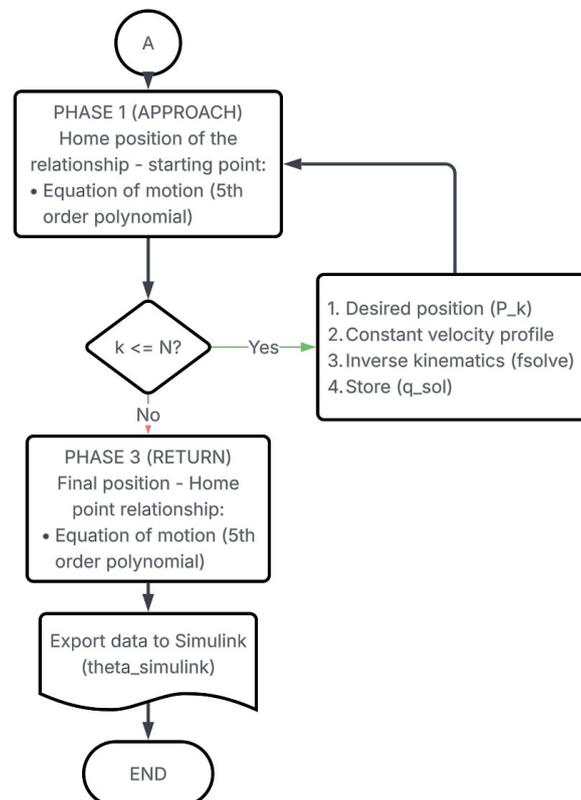
Once the geometric path is defined, the algorithm proceeds to the motion execution phase via connector "A", as detailed in Figure 13. To ensure mechanical safety and prevent abrupt accelerations, the initial transition from the relationship's home position

to the starting point (**Phase 1: Approach**) is governed by a **5th Order Polynomial** equation of motion.

The core of the process is the iterative loop controlled by the decision block  $k \leq N$ . Here,  $k$  represents the current step index and  $N$  is the total number of points in the discretized trajectory. As long as  $k \leq N$ , the loop executes the following steps for the welding path:

1. **Desired Position ( $P_k$ ):** The target coordinates are extracted.
2. **Constant Velocity Profile:** Time segments are calculated to maintain the user-defined speed.
3. **Inverse Kinematics:** The numerical solver (*fsolve*) computes the required joint angles ( $q_{sol}$ ).

When the condition  $k \leq N$  is met (indicating the path is complete), the system initiates **Phase 3 (Return)**, which moves the robot back to the home relationship position using a smooth 5th-order polynomial profile. Finally, the computed joint data is consolidated and exported to the MATLAB Workspace as `theta_simulink` for simulation.



**Figure 13.** Flowchart Part 2: Execution Loop, Quintic Transitions, and Data Export.

### 2.2.3.2. Control Architecture and Simulation

Once the joint-angle signals are generated (exported as *theta\_simulink*), the validation phase is conducted in Simulink/Simscape. Maintaining adequate control of end-effector speed and acceleration is fundamental for weld quality, as discussed in real-time monitoring studies [2, 27, 28]. To assess this, a comparative architecture was designed (Figure 14), where the reference signals are sent simultaneously to an “Ideal” kinematic model and a “Real” physical model that accounts for mass and inertia.

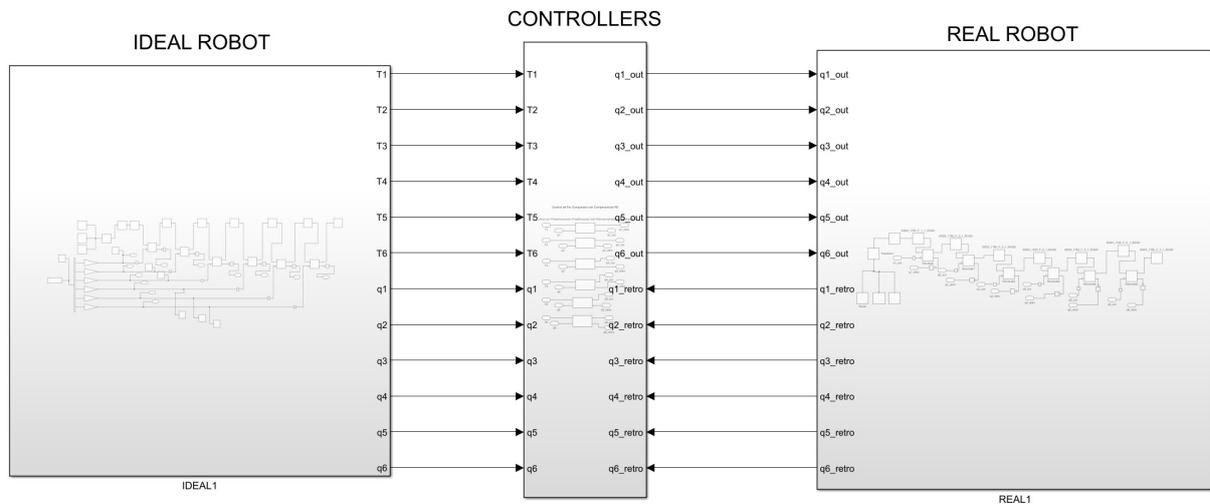


Figure 14. Simulation Architecture: Ideal vs. Real

The internal structure of the Simulink model connects the kinematic transforms with the rigid body blocks, creating a chain of coordinate systems that represents the serial arm, as detailed in Figure 15.

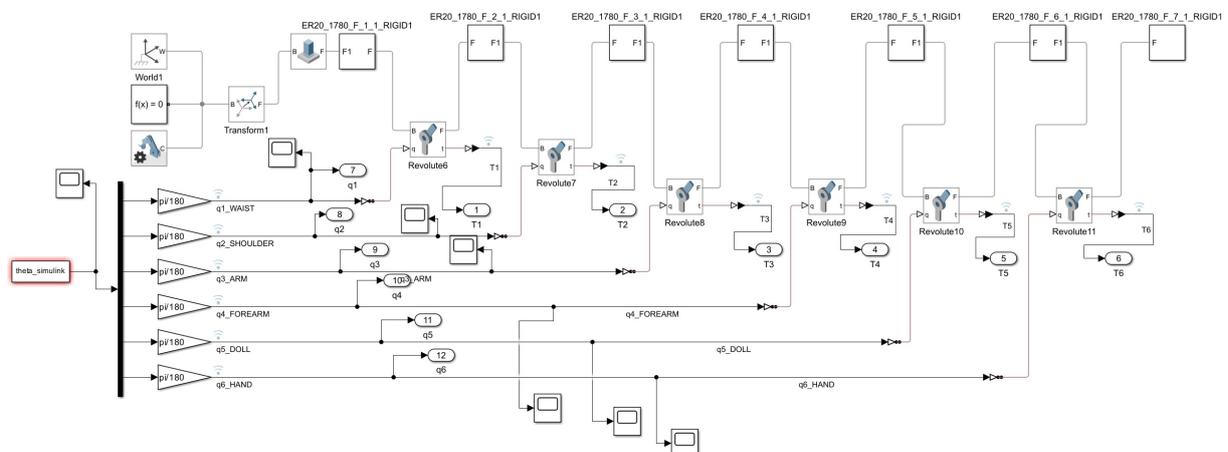
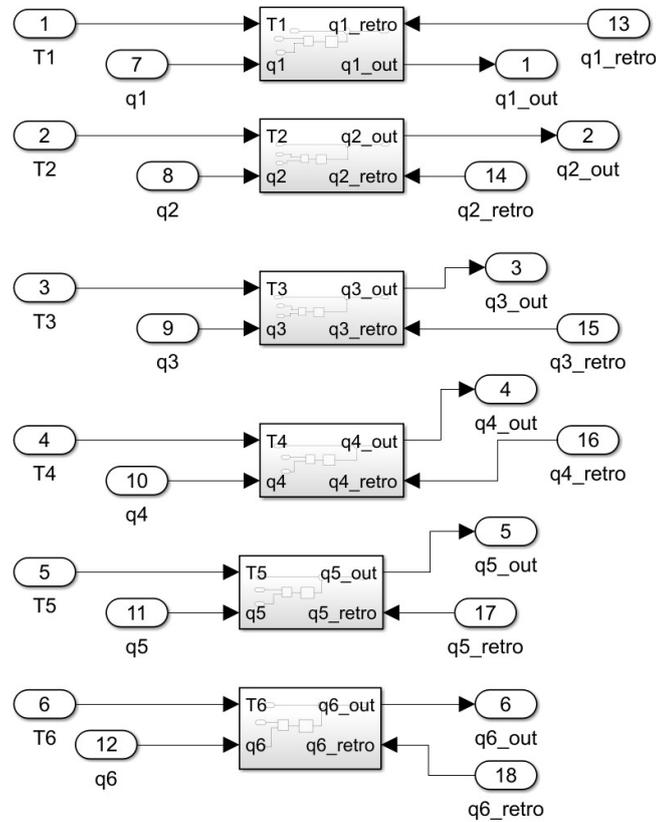


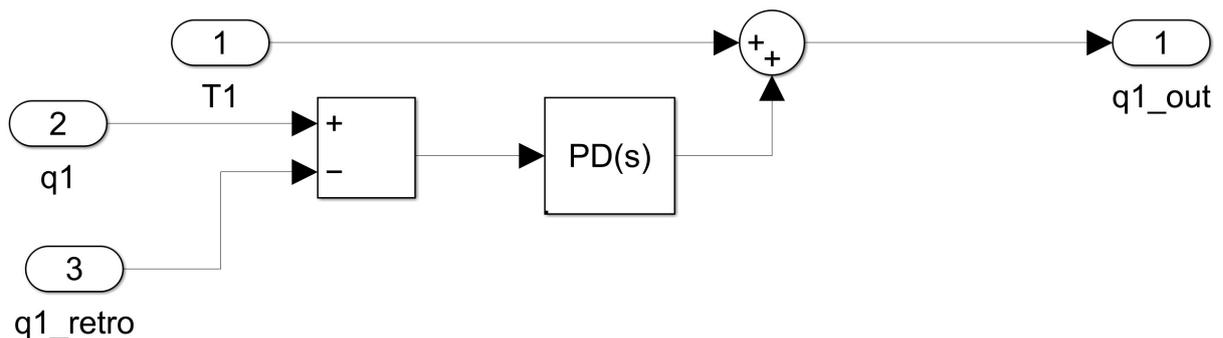
Figure 15. Simulink Block: Ideal Robot

The control strategy is decentralized, meaning each joint ( $J_1$  to  $J_6$ ) is governed by an independent control loop, as illustrated in Figure 16. This modular approach facilitates the tuning of individual gains for each actuator.



**Figure 16.** Simulink Block: Control loops for joints.

Specifically, a PD (Proportional-Derivative) controller with feedforward compensation is employed (Figure 17). This controller compares the desired position ( $q$ ) against the feedback from the physical plant ( $q_{retro}$ ) to compute the necessary torque ( $T$ ), ensuring that the robotic arm executes precise angular corrections to maintain the tool within the required tolerance.



**Figure 17.** PD Controller + Feedforward Structure

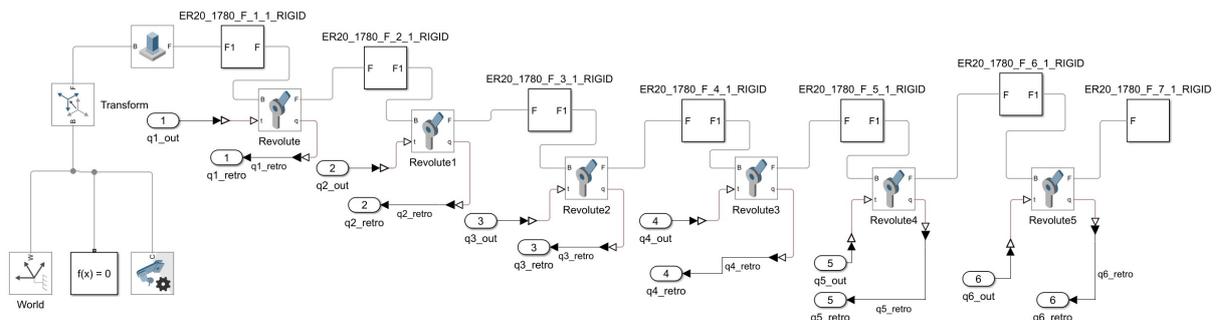
This control structure implements a **Computed Torque Control** strategy with PD compensation architecture. Unlike a simple PID regulator, this system relies primarily on a dynamic feedforward term ( $\tau_{ff}$ ), calculated from the ideal inverse dynamics, which anticipates the torques required to overcome gravity, inertia, and Coriolis forces. The control law is defined as:

$$\tau_i = \tau_{ff,i} + K_{p,i} \cdot e_i + K_{d,i} \cdot \dot{e}_i \quad (2.1)$$

Where  $K_{p,i}$  acts as a virtual stiffness and  $K_{d,i}$  provides electronic damping.

It is important to note that, in this specific simulation, the feedforward model demonstrated high fidelity in predicting the required torque. Consequently, the proportional action ( $K_p$ ) was sufficient to correct minor position errors, while the inherent mechanical damping modeled in the Simscape joints rendered high derivative gains unnecessary. This validates the accuracy of the mathematical model derived in the early stages, as the controller effectively operates by relying on the physics-based pre-calculation rather than reactive error correction.

Finally, to close the control loop, the physical behavior of the manipulator is simulated using the **Simscape Multibody** environment. Unlike simple kinematic animations, this block models the true dynamics of the system, assigning physical properties such as mass, center of gravity, and inertia tensors to each link. This setup allows for a rigorous assessment of whether the actuators possess sufficient torque to drive the 16 kg payload through the calculated trajectories, accounting for non-linear effects like gravity and joint friction.



**Figure 18.** Simulink Block: Real Robot

The execution of the simulation in this virtual environment serves as a qualitative validation step. Visual inspection confirms that the manipulator successfully tracks the spatial coordinates defined in the input signal (*theta\_simulink*), maintaining the tool orientation within the required welding constraints. The smooth motion observed, devoid of vibrations or kinematic singularities, corroborates the effectiveness of the feedforward-dominant control strategy and confirms the structural capability of the arm. This successful correlation between the mathematical generator and the physical simulator provides the necessary reliability to proceed with the quantitative analysis of the trajectory errors in the following stage.

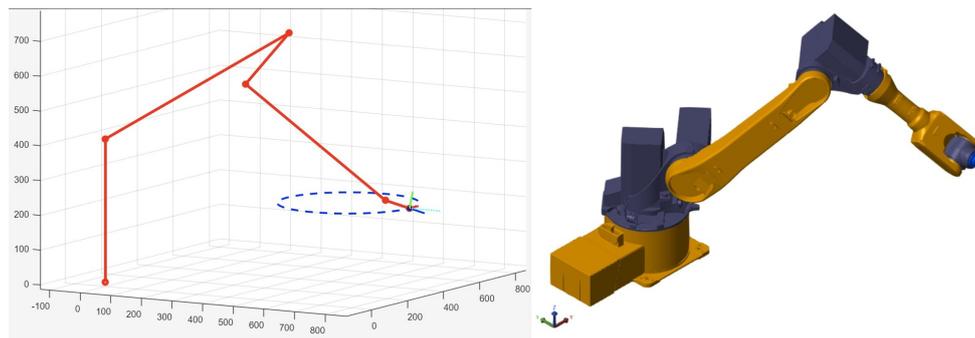
## 2.3. STAGE III: SYSTEM VERIFICATION AND VALIDATION

### 2.3.1. Simulation and Validation

To perform the simulation and validate the movements of the predefined shapes, a code was used to generate a 3D animation of the robotic arm following trajectories calculated via iterative inverse kinematics. The model is defined symbolically using the Denavit–Hartenberg parameters from Table 1, and the homogeneous transformations of each link are converted into numerical functions for fast evaluation of joint configurations. An inverse kinematics method based on *fsolve* iteratively adjusts the joint values to reach the desired positions and orientations. The visualization module computes each joint's position and interpolates the trajectory points to display the motion frame by frame. This setup allows the robotic arm to execute the circular, square, and linear Z-axis trajectories accurately, as shown in Figures 19, 20, and 21.

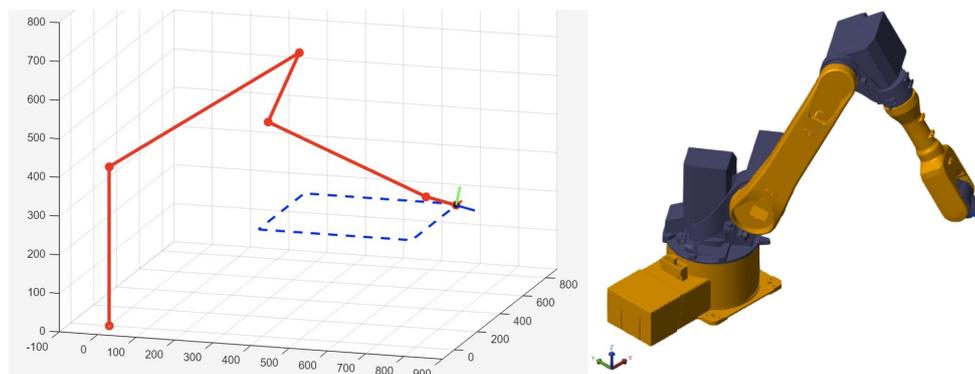
- **Circular Trajectory:** is generated by interpolating three-dimensional points along a smooth curve within the chosen plane. Each point is sent to the inverse kinematics solver, which calculates the required joint configuration so that the end-effector maintains its orientation while following the curved path. As shown in Figure 19, this approach allows for assessing motion smoothness and stability of orientation throughout the trajectory. According to [8], such test scenarios are widely used to simulate complex processes like welding, enabling motion valida-

tion without the need for physical hardware.



**Figure 19.** 3D Representation of Circular Motion.

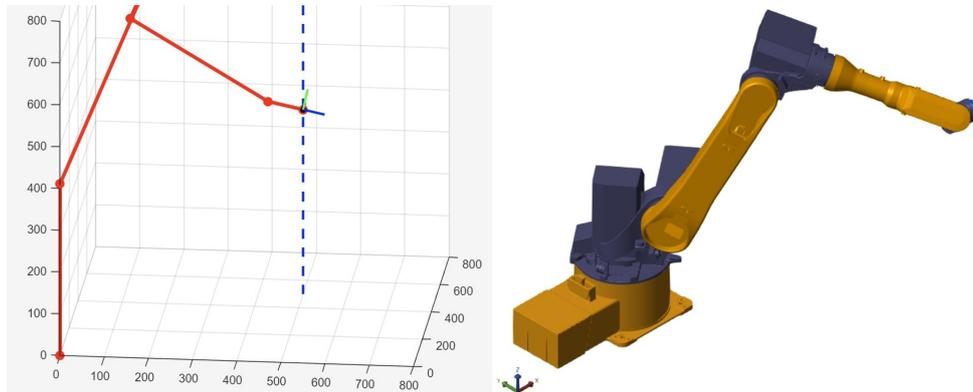
- **Square Trajectory:**, the path is constructed from consecutive straight segments, each discretized into equally spaced points. The inverse kinematics solver computes each point to ensure the robot maintains consistent velocity, orientation, and smooth transitions at sharp corners. In Figure 20, the structured sequence of segments forming the square contour is shown, which is useful for analyzing corner stability. Precision evaluation through comparison with experimental data, as indicated in [4], allows validation of the geometric reliability of the generated motion.



**Figure 20.** 3D Representation of Square Motion.

- **Linear Movement Along the Z-Axis:** is obtained by keeping X and Y fixed while Z varies uniformly, resulting in a pure vertical trajectory. Each point along the line is converted into a stable and aligned joint configuration, producing a straight displacement without lateral deviations. Figure 21 shows the straight path characteristic of this movement, ideal for analyzing axial stability. As studies like [24]

suggest, metrics such as mean squared error can quantify the precision of the end-effector tracking in this type of trajectory.



**Figure 21.** 3D Representation of Linear Movement Along the Z-Axis Motion.

### 2.3.2. Actuator Sizing Criteria and Service Factors

The selection of actuators involves applying a *Service Factor* ( $K_s$ ) to the loads calculated under **Critical Operating Conditions**. These load values were validated through extensive dynamic simulations performed across two distinct operational workspaces to ensure reliability under different geometric configurations.

The specific simulation results supporting these values are detailed in the Appendices. Tables A.1, A.2, and A.3 present the torque measurements for Circular, Square, and Linear trajectories within *Workspace 1*, while Tables B.1, B.2, and B.3 detail the corresponding results for *Workspace 2*.

Based on the peak values observed in these simulations and mechanical design principles established in [29], the following safety factors were defined:

1. **Gravitational Axes (J2, J3, J5):** For joints primarily supporting static loads, a Safety Factor of  $FS = 1.3$  was selected. This aligns with industry recommendations to maintain the continuous RMS torque below 80% of the motor's rated capacity, preventing thermal overload during holding operations [30].
2. **Dynamic/Inertial Axes (J1, J4):** For the base (J1), which is subject to high start-up friction and inertial shock loads identified in the *Workspace 1* simulations (Tables A.1-A.3), a conservative factor of  $FS = 3.3$  was applied. This margin is con-

sistent with AGMA standards for "Heavy Shock" loads [31], ensuring the actuator can deliver the required peak torque ( $> 450$  Nm) without saturation.

### 2.3.3. Analytical Torque Calculation Methodology

The required torque rating for the selected motor ( $\tau_{motor}$ ) is derived by applying the design safety factors to the calculated dynamic load ( $\tau_{calc}$ ), obtained via the Inverse Dynamics method. The governing equation is:

$$\tau_{motor} = \tau_{calc} \cdot FS = (\tau_{grav} + \tau_{inertial} + \tau_{friction}) \cdot FS \quad (2.2)$$

#### 2.3.3.1. Wrist Unit Analysis (J4 – J6)

The wrist unit handles the direct manipulation of the welding torch.

- **Joint 6 (Hand):** The load is dominated by cable stiffness and friction rather than pure inertia.
- **Joint 5 (Doll):** Must overcome the gravitational torque of the offset torch in a cantilever configuration.
- **Joint 4 (Forearm Roll):** Subject to cross-inertial loads (gyroscopic effects) during rapid curved movements due to the 0.20 m tool offset.

#### 2.3.3.2. Sample Calculation: Joint 2 (Shoulder)

To demonstrate the sizing methodology applied to the system, the specific calculation for Joint 2 is detailed below. This joint represents a critical case for gravitational holding torque.

1. **Determination of Calculated Load ( $\tau_{calc}$ ):** Based on the dynamic simulation of the kinematic chain (including link masses and the 10 kg payload), the peak torque required to maintain static equilibrium was determined to be:

$$\tau_{calc,J2} = 301.9 \text{ Nm}$$

2. **Application of Safety Factor ( $FS$ ):** As established in the design criteria for gravitational axes, a factor of  $FS = 1.3$  is applied [29].
3. **Calculation of Motor Torque Capacity ( $\tau_{motor}$ ):** Applying the design factor to the calculated load:

$$\tau_{motor,J2} = \tau_{calc,J2} \times FS$$

$$\tau_{motor,J2} = 301.9 \text{ Nm} \times 1.3 = 392.47 \text{ Nm}$$

Rounding for specification purposes:

$$\tau_{motor,J2} \approx 392.5 \text{ Nm}$$

**Note:** This identical calculation procedure was applied to all remaining degrees of freedom (J1, J3-J6) to determine the final actuator specifications.

### 2.3.4. Summary of Sizing Results

Table 2 summarizes the sizing results. The **Calculated Torque** column represents the physical load derived from the critical simulations, while the **Motor Torque** column indicates the minimum capacity required for the actuator selection.

**Table 2.** Actuator Sizing Requirements based on Critical Simulation Conditions

Joint	Primary Load	Motor Torque ( $\tau_{calc}$ [Nm])	Design Factor ( $FS$ )	Calculated Torque ( $\tau_{motor}$ [Nm])
<b>J1 (Base)</b>	Inertial	140.0	<b>3.3</b>	<b>462.0</b>
<b>J2 (Shoulder)</b>	Gravitational	301.9	1.3	<b>392.5</b>
<b>J3 (Elbow)</b>	Gravitational	129.3	1.3	<b>168.1</b>
<b>J4 (Forearm)</b>	Gyroscopic	25.1	3.0	<b>75.3</b>
<b>J5 (Doll)</b>	Gravitational	20.1	1.3	<b>26.1</b>
<b>J6 (Hand)</b>	Friction	2.6	1.5	<b>3.9</b>

## Chapter 3

### RESULTS

The simulation evaluated the robot's dynamic behavior across three representative trajectories: circular, square, and linear (Z-axis), utilizing the Denavit–Hartenberg parameters established in Table 1. To reflect real-world industrial scenarios based on standard [6], two operating modes were compared:

- **Continuous Mode (3.2 mm spacing):** Strictly constrained to a travel speed of **8 mm/s** to ensure adequate heat input and bead formation, simulating a thermally constrained welding process.
- **Intermittent Mode (40 mm spacing):** Allowed to utilize higher rapid-traverse speeds during non-welding transitions, simulating a rapid positioning task.

Performance metrics, including maximum torque peaks ( $N \cdot m$ ) and trajectory tracking errors, were computed via MATLAB for all six joints ( $J1–J6$ ) to identify critical stress points. While detailed datasets are provided in the Appendices, this section summarizes the critical findings.

#### 3.1. CIRCULAR TRAJECTORY

To validate the circular trajectory, an experimental protocol was designed to adjust the radius ( $R$ ) dynamically while adhering to the velocity constraints defined above. The analysis compares the high-precision continuous tracking required for a welding bead against the point-to-point motion used for spot welding or roughing.

##### 3.1.1. Dynamic Torque Validation

To evaluate the dynamic demands placed on the actuators during the execution of the circular trajectory, the maximum torque ( $\tau_{max}$ ) was monitored at each of the six joints of the manipulator for the two working scenarios. The comparison of these results is

presented in Table 5, which contrasts the values obtained under the **Continuous configuration** (step of 3.2 mm) with those obtained under the **Intermittent configuration** (operating separation of 40 mm):

**Table 3.** Maximum Torque in Circular Trajectory: Continuous vs. Intermittent

No. (Test)	Size (Radius) [m]	J1 (Waist) [N · m]	J2 (Shoulder) [N · m]	J3 (Arm) [N · m]	J4 (Forearm) [N · m]	J5 (Doll) [N · m]	J6 (Hand) [N · m]
1	0.010	450 / 320	240 / 260	140 / 50	70 / 55	7.0 / 5.0	2.0 / 110
2	0.015	230 / 180	155 / 120	90 / 30	42 / 5	5.0 / 3.0	2.0 / 12
3	0.020	170 / 180	100 / 120	30 / 30	25 / 5	4.0 / 3.0	2.0 / 12
4	0.030	180 / 180	102 / 120	30 / 35	12 / 8	3.0 / 2.0	2.0 / 12
5	0.050	170 / 160	100 / 100	30 / 30	4 / 5	3.0 / 1.5	2.0 / 12
6	0.070	160 / 160	100 / 100	30 / 30	1.8 / 6	2.4 / 1.4	2.0 / 12
7	0.100	160 / 155	100 / 100	30 / 30	2 / 6	3.0 / 1.2	2.5 / 12
8	0.150	180 / 130	120 / 100	30 / 30	1.8 / 5	2.0 / 1.0	2.5 / 12
9	0.200	180 / 120	120 / 95	35 / 32	1.8 / 7	1.6 / 1.2	2.5 / 12
10	0.300	165 / 85	140 / 85	70 / 40	2.5 / 6	2.0 / 0.6	2.4 / 12

*Note: Torque values are presented as: Continuous Mode / Intermittent Mode.*

The analysis of the data shows that the **Continuous configuration** (3.2 mm) places a significantly higher mechanical load on the robot, especially during the initial movements where the base joint (J1) reached up to  $450 \text{ N} \cdot \text{m}$ , compared to the  $320 \text{ N} \cdot \text{m}$  observed with the Intermittent strategy. Although the **Continuous Mode** operates at a lower velocity (6 mm/s), the requirement to strictly follow points that are very close together forces the manipulator to perform rapid and continuous micro-corrections to maintain path fidelity, increasing motor effort.

During larger circular trajectories, the main load shifts to joints J2 and J3 due to gravity; however, the intermittent mode remains more efficient by keeping overall dynamic demands lower. The only exception is the wrist joint (J6), which increases its torque to approximately  $12 \text{ N} \cdot \text{m}$  (compared to  $\sim 2 \text{ N} \cdot \text{m}$  in the **Continuous Mode**) due to the need to maintain a stiffer posture of the welding tool during the longer 40 mm displacements.

### 3.1.2. Evaluation of Trajectory Execution Accuracy

To validate the operational performance, the analysis focused on the positioning accuracy of the end-effector (Tool Center Point) by quantifying the error ( $E_p$ ) as the Euclidean distance between the programmed target coordinates ( $P_{target}$ ) and the actual coordinates ( $P_{actual}$ ) in the 3D workspace. This metric captures the cumulative error of the kinematic chain, allowing for a direct assessment of spatial deviation magnitude as summarized in Table 6, which presents the maximum deviations observed under the most demanding test scenarios.

**Table 4.** Precision Error Distribution Across the 6 Joints (Test 4)

Joint	Mechanical Function	Error (%)	Error (%)
		Cont. (3.2 mm)	Int. (40 mm)
<b>J1</b>	Waist (Rotation)	0.02%	0.16%
<b>J2</b>	Shoulder (Lift)	0.39%	0.11%
<b>J3</b>	Arm (Reach)	0.34%	0.67%
<b>J4</b>	Forearm Rotation	0.43%	1.06%
<b>J5</b>	Doll Rotation	<b>0.83%</b>	<b>2.89%</b>
<b>J6</b>	Hand (End-Effector)	0.18%	2.87%

The data clearly differentiates the behavior of the positioning joints (**J1–J3**) from that of the orientation joints (**J4–J6**). The joints responsible for placing the robot in X–Y–Z maintain stable accuracy in both strategies, typically staying below 0.5% error. Interestingly, **J2** performs slightly better under the intermittent strategy, likely due to reduced high-frequency vibrations that improve its control response.

In contrast, the orientation joints exhibit a significant loss of accuracy when the 40 mm spacing is applied. Both **J5** and **J6** reach error values close to 3%, showing that the intermittent strategy significantly increases the angular demand on the robot's wrist. This indicates that while overall positioning remains consistent, the end-effector orientation becomes more sensitive to dynamic variations and the higher angular accelerations required during longer steps.

## 3.2. CIRCULAR TRAJECTORY

To validate the circular trajectory, an experimental protocol was designed to adjust the radius ( $R$ ) dynamically while adhering to the velocity constraints defined above. The analysis compares the high-precision continuous tracking required for a welding bead against the point-to-point motion used for spot welding or roughing. The complete experimental dataset comparing these scenarios corresponds to the results recorded in **Table A.1** (Workspace 1) and **Table B.1** (Workspace 2) of the Appendices.

### 3.2.1. Dynamic Torque Validation

To evaluate the dynamic demands placed on the actuators during the execution of the circular trajectory, the maximum torque ( $\tau_{max}$ ) was monitored at each of the six joints of the manipulator for the two working scenarios. The comparison of these results is presented in Table 5, which contrasts the values obtained under the **Continuous configuration** (step of 3.2 mm) with those obtained under the **Intermittent configuration** (operating separation of 40 mm).

**Table 5.** Maximum Torque in Circular Trajectory: Continuous vs. Intermittent

No. (Test)	Size (Radius) [m]	J1 (Waist) [N · m]	J2 (Shoulder) [N · m]	J3 (Arm) [N · m]	J4 (Forearm) [N · m]	J5 (Doll) [N · m]	J6 (Hand) [N · m]
1	0.010	450 / 320	240 / 260	140 / 50	70 / 55	7.0 / 5.0	2.0 / 110
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7	0.100	160 / 155	100 / 100	30 / 30	2 / 6	3.0 / 1.2	2.5 / 12
8	0.150	180 / 130	120 / 100	30 / 30	1.8 / 5	2.0 / 1.0	2.5 / 12
9	0.200	180 / 120	120 / 95	35 / 32	1.8 / 7	1.6 / 1.2	2.5 / 12
10	0.300	165 / 85	140 / 85	70 / 40	2.5 / 6	2.0 / 0.6	2.4 / 12

*Note: Torque values are presented as: Continuous Mode / Intermittent Mode.*

The analysis indicates that the **Continuous configuration** (3.2 mm) imposes significantly higher mechanical loads, particularly on the base (J1), which peaked at 450  $N \cdot m$  versus 320  $N \cdot m$  in the Intermittent strategy. Despite the lower velocity (6 mm/s), the need for rapid micro-corrections to maintain path fidelity drives up motor effort. While

gravity dominates J2 and J3 loads in larger radii, the intermittent mode remains dynamically more efficient, except for the wrist (J6); here, torque rises to  $\sim 12 N \cdot m$  (vs.  $\sim 2 N \cdot m$ ) to stabilize the tool during the longer 40 mm displacements.

### 3.2.2. Evaluation of Trajectory Execution Accuracy

To validate the operational performance, the analysis focused on the positioning accuracy of the end-effector (Tool Center Point) by quantifying the error ( $E_p$ ) as the Euclidean distance between the programmed target coordinates ( $P_{target}$ ) and the actual coordinates ( $P_{actual}$ ) in the 3D workspace. This metric captures the cumulative error of the kinematic chain, allowing for a direct assessment of spatial deviation magnitude as summarized in Table 6.

**Table 6.** Precision Error Distribution Across the 6 Joints (Test 4)

Joint	Mechanical Function	Error (%) Cont. (3.2 mm)	Error (%) Int. (40 mm)
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<b>J3</b>	Arm (Reach)	0.34%	0.67%
<b>J4</b>	Forearm Rotation	0.43%	1.06%
<b>J5</b>	Doll Rotation	<b>0.83%</b>	<b>2.89%</b>
<b>J6</b>	Hand (End-Effector)	0.18%	2.87%

The data clearly differentiates the behavior of the positioning joints (**J1–J3**) from that of the orientation joints (**J4–J6**). The joints responsible for placing the robot in X–Y–Z maintain stable accuracy in both strategies, typically staying below 0.5% error. Interestingly, **J2** performs slightly better under the intermittent strategy, likely due to reduced high-frequency vibrations that improve its control response. In contrast, the orientation joints exhibit a significant loss of accuracy when the 40 mm spacing is applied. Both **J5** and **J6** reach error values close to 3%, showing that the intermittent strategy significantly increases the angular demand on the robot’s wrist.

### 3.3. SQUARE TRAJECTORY

The system's performance was evaluated using the **Side Length** ( $L$ ) as the primary variable, comparing the **Continuous** strategy (3.2 mm) against the **Intermittent** strategy (40 mm) to analyze the robot's behavior at sharp  $90^\circ$  corners. A critical factor in this comparison is the velocity profile: while the **Continuous Mode** was constrained to a constant welding speed of 6 mm/s, the **Intermittent Mode** utilized rapid positioning speeds for the straight segments.

The complete experimental dataset comparing cycle times corresponds to the results recorded in **Table A.2** (Workspace 1) and **Table B.2** (Workspace 2) of the Appendices. The analysis of this data reveals that performance depends directly on geometry size. For small squares ( $L = 0.045$  m), the difference is negligible as the inertial effort of corner braking dominates the cycle. However, for larger trajectories ( $L = 0.400$  m), the intermittent strategy effectively exploits the long straight segments to accelerate beyond the process limit, achieving a **46% reduction in total cycle time** compared to the continuous mode.

#### 3.3.1. Dynamic Torque Validation

The study of the Maximum Torque ( $\tau_{max}$ ) reveals a different behavior compared to the circular path: due to the geometry of the square, the robot must perform sharp decelerations when passing through each corner. As shown in Table 7, the **Intermittent** strategy (40 mm) imposes a significantly higher load on the robot's base joint (Joint 1), especially in medium and large trajectories. This indicates that long straight segments combined with  $90^\circ$  direction changes generate stronger inertial forces than those present in the smooth and constant 3.2 mm motion.

**Table 7.** Maximum Torque in Square Trajectory: Continuous vs. Intermittent

No. (Test)	Side (m)	J1 (Waist) [N · m]	J2 (Shoulder) [N · m]	J3 (Arm) [N · m]	J4 (Forearm) [N · m]	J5 (Doll) [N · m]	J6 (Hand) [N · m]
1	0.045	175 / 175	110 / 110	30 / 35	2 / 2	2 / 2	2 / 1
2	0.050	225 / 230	120 / 115	35 / 35	2 / 2	2 / 2	3 / 1
3	0.060	230 / 230	120 / 115	35 / 35	2 / 2	2 / 2	3 / 1
4	0.070	180 / <b>230</b>	120 / 115	35 / 35	2 / 2	2 / 2	3 / 1
5	0.095	240 / <b>300</b>	120 / 110	35 / 35	2 / 3	2 / 2	3 / 2
6	0.100	240 / <b>300</b>	120 / 110	35 / 35	2 / 3	2 / 2	3 / 2
7	0.150	240 / <b>300</b>	120 / 110	35 / 35	3 / 3	2 / 2	3 / 2
8	0.200	300 / <b>340</b>	100 / 100	35 / 75	3 / 3	2 / 2	3 / 2
9	0.300	270 / <b>340</b>	100 / 100	70 / 75	3 / 3	2 / 2	3 / 2
10	0.400	260 / <b>340</b>	<b>135 / 100</b>	<b>150 / 75</b>	3 / 3	6 / 2	3 / 2

*Note: Torque values are presented as: Continuous Mode / Intermittent Mode.*

The analysis reveals a clear trade-off in the robot's mechanical load: as the size of the square increases (from approximately 0.070 m onward), the intermittent strategy places significantly higher demand on the Base (J1), which must exert more force to stop and redirect the motion at each 90° corner; however, this added load brings a notable advantage to the rest of the arm, since the joints that carry most of the weight (J2 and J3) experience reduced stress, with the elbow torque dropping to nearly half in the largest test (Test 10).

### 3.3.2. Evaluation of Trajectory Execution Accuracy

Finally, the trajectory quality was assessed by examining the positioning error. Unlike the circular trajectory, where the main challenge was maintaining a constant curvature, the square trajectory demands stable linear motion along each side and accurate reorientation at every corner. The results reveal a clear functional split: the joints responsible for global positioning (J1, J2, and J3) preserve nearly identical stability across both strategies, while the wrist joint (J5) exhibits a noticeable improvement when using the intermittent method.

**Table 8.** Accuracy Error Distribution Across the 6 Joints

Joint	Mechanical Function	Error (%) Cont. (3.2 mm)	Error (%) Int. (40 mm)
J1	Waist (Rotation)	0.03%	0.02%
J2	Shoulder (Elevation)	0.03%	0.04%
J3	Arm (Reach)	0.10%	0.14%
J4	Forearm Rotation	0.00%	0.00%
J5	Doll Rotation	<b>2.40%</b>	<b>1.24%</b>
J6	Hand (End-Effector)	0.39%	0.13%

When evaluating the trajectory accuracy, the results are highly favorable for the intermittent strategy, particularly in the distal section of the robot. While the main axes (J1, J2, and J3) maintain impeccable precision in both scenarios, a substantial improvement is observed in the wrist assembly: both the orientation joint (J5) and the end-effector (J6) achieved significantly cleaner motion, reducing their errors drastically (J5 decreased by half and J6 dropped to a minimum of 0.13%), while J4 remained stable with practically negligible deviations.

### 3.4. LINEAR TRAJECTORY (Z-AXIS)

The behavior of the manipulator was examined during a purely vertical trajectory along the Z-axis, a physically demanding scenario where the robot works directly against gravitational force ( $g$ ). The study compares the system's response when performing upward motions under the **Continuous** strategy (3.2 mm, physically constrained to 8 mm/s) versus the **Intermittent** strategy (40 mm, utilizing rapid traverse).

The complete experimental dataset comparing cycle times corresponds to the results recorded in **Table A.3** (Workspace 1) and **Table B.3** (Workspace 2) of the Appendices. In terms of speed, the intermittent approach maintains an advantage over longer distances precisely because it bypasses the process velocity limit imposed on the continuous mode. For short movements ( $< 0.4$  m), the difference is slight; however, in the longest displacement (0.9 m), the intermittent strategy regains effectiveness, achieving a 13% reduction in total execution time by utilizing high-speed travel between points.

### 3.4.1. Dynamic Torque Validation

Unlike the square trajectory, where pauses give the arm brief relief, vertical movement behaves differently: **gravity penalizes stops**. Table 9 presents the maximum torques recorded under both strategies. It highlights how the joints responsible for elevation, particularly the Shoulder (J2), are significantly affected by the intermittent motion. Each stop every 40 mm causes the robot to lose upward momentum, forcing the joints to repeatedly overcome static friction and the weight of the arm.

**Table 9.** Maximum Torque in Vertical Trajectory: Continuous vs. Intermittent

No. (Test)	Height (m)	J1 (Waist) [N · m]	J2 (Shoulder) [N · m]	J3 (Arm) [N · m]	J4 (Forearm) [N · m]	J5 (Doll) [N · m]	J6 (Hand) [N · m]
1	0.05	380 / 400	325 / 300	105 / 98	4 / 4	5 / 6	1 / 1
2	0.10	380 / 400	300 / 300	95 / 98	4 / 4	5 / 6	1 / 1
3	0.20	380 / 380	275 / 275	85 / 90	3 / 4	5 / 5	1 / 1
4	0.30	365 / 365	240 / <b>300</b>	75 / <b>115</b>	4 / 4	5 / 5	1 / 1
5	0.40	340 / 350	265 / <b>340</b>	90 / <b>115</b>	3 / 4	5 / 5	1 / 1
6	0.50	330 / 310	270 / <b>360</b>	90 / <b>110</b>	3 / 4	4 / 5	1 / 1
7	0.60	270 / 230	265 / <b>360</b>	85 / <b>120</b>	3 / 3	3 / 5	1 / 1
8	0.70	230 / 230	290 / <b>360</b>	100 / <b>120</b>	2 / 3	4 / 5	1 / 1
9	0.80	190 / 180	290 / <b>350</b>	100 / <b>125</b>	2 / 3	4 / 5	1 / 1
10	0.90	150 / 170	270 / <b>320</b>	110 / <b>125</b>	2 / 3	4 / 5	1 / 1

*Note: Torque values are presented as: Continuous Mode / Intermittent Mode.*

The data clearly shows how the intermittent strategy significantly affects the joints responsible for elevation, particularly the Shoulder (J2) and Elbow (J3). As the robot stops every 40mm, it loses its accumulated upward momentum, forcing the joints to repeatedly overcome static friction and the arm's weight.

### 3.4.2. Evaluation of Trajectory Execution Accuracy

Positioning accuracy was evaluated, showing that stability is remarkably high for both strategies, with marginal errors rarely exceeding 1%. Table 10 demonstrates that there are no significant differences in the quality of the vertical trajectory. Both J5 (Wrist) and J6 (Flange) maintain consistent error levels, around 0.6% - 0.9%. This indicates that, although the intermittent strategy requires higher torque (energy), it does not compromise the geometric accuracy of the path.

**Table 10.** Distribution of Positioning Error Across the 6 Joints

Joint	Mechanical Function	Error (%) Cont. (3.2 mm)	Error (%) Int. (40 mm)
<b>J1</b>	Waist (Rotation)	0.03%	0.04%
<b>J2</b>	Shoulder (Elevation)	0.04%	0.04%
<b>J3</b>	Arm (Reach)	0.47%	0.48%
<b>J4</b>	Forearm Rotation	0.65%	0.59%
<b>J5</b>	Doll Rotation	<b>0.53%</b>	0.68%
<b>J6</b>	Hand (End-Effector)	0.95%	0.96%

In conclusion, for the vertical linear trajectory, the results reveal a trade-off: the intermittent strategy achieves a moderate time reduction (13%) thanks to rapid positioning speeds, but imposes a **substantial energy penalty** on the Shoulder and Elbow motors.

### 3.5. GENERAL MULTIVARIATE VALIDATION

This section integrates the results from the Circular, Square, and Linear trajectories. To rigorously validate the system, the analysis focuses on the **absolute maximum loads** experienced by the robot across all operational scenarios. This "Worst-Case Scenario" approach ensures that the dynamic model and the selected actuators are capable of withstanding the highest stresses generated, regardless of the trajectory geometry.

#### 3.5.1. Global Dynamic Validation: Worst-Case Analysis

Table 11 presents a comparison between the **Theoretical Torque** (calculated via Euler-Lagrange) and the **Maximum Simulated Torque** recorded during the entire experimental phase. The table highlights the highest stress peak recorded for each joint, regardless of which trajectory generated it, providing a safety margin validation for the motor selection.

**Table 11.** Global Validation: Maximum Torques Across All Trajectories

Joint	Calculated Torque ( $\tau_{calc}$ ) [ $N \cdot m$ ]	Simulated Torque ( $\tau_{sim}$ ) [ $N \cdot m$ ]	Relative Error [%]
J1	430.5	<b>450.0</b>	4.3%
J2	342.0	<b>360.0</b>	5.0%
J3	142.8	<b>150.0</b>	4.8%
J4	65.5	<b>70.0</b>	6.4%
J5	6.5	<b>7.0</b>	7.1%
J6	102.0	<b>110.0</b>	7.2%

### 3.5.2. Analysis of Critical Stress Points

The peak values presented above did not occur simultaneously; rather, they correspond to specific geometric conditions where the physical demands on each joint were maximized. The origin of these critical loads is detailed below:

- **Waist (J1):** The maximum torque of  $450 N \cdot m$  was recorded during the **Circular Trajectory**. This is attributed to the continuous change in the acceleration vector required to follow the curvature. Even at the constrained welding speed (6 mm/s), the high rotational inertia of the arm demands significant torque to maintain path fidelity during these constant directional updates.
- **Shoulder (J2):** The peak load of  $360 N \cdot m$  occurred during the **Vertical Linear Trajectory (Z-Axis)**. In this scenario, the motor must overcome the direct gravitational load to lift the entire arm structure from a standstill, without the aid of momentum.
- **Arm (J3):** The maximum stress of  $150 N \cdot m$  was observed in the **Square Trajectory**. This peak corresponds to the furthest corners of the square, where the lever arm is fully extended, maximizing the moment of force required to hold the forearm position.
- **Forearm, Doll and Hand (J4–J6):** The orientation joints experienced their highest demands during **Small-Radius Circular Trajectories**. The need for high-frequency corrections to maintain the welding torch orientation relative to the path resulted in instantaneous torque shocks, particularly in the end-effector (J6).

Despite the complexity of these varied scenarios, the error between the theoretical calculation and the simulation remains consistently below 8%. The slight increase in simulated torque is expected due to the inclusion of joint friction and complex inertia tensors in the CAD model, confirming that the dynamic model is robust and reliable for operational prediction.

## Chapter 4

### CONCLUSIONS AND RECOMMENDATIONS

#### 4.1. CONCLUSIONS

- A robotic arm for automated welding was simulated in two working modes. In the main joints ( $J_1$ – $J_3$ ), both modes had errors below **0.5%**. However, the intermittent mode caused almost a 3% error in the wrist ( $J_4$ – $J_6$ ). Therefore, the continuous mode is the best choice for welding without deviations.
- The design and chosen motors proved to be highly resistant. They easily supported the maximum forces of **450 Nm** at the base ( $J_1$ ) and **360 Nm** at the shoulder ( $J_2$ ). The control system also kept the arm stable against gravity, making it ideal for the job.
- The geometric calculations used to guide the robot proved to be completely reliable. When testing different shapes, the parts responsible for positioning the arm ( $J_1$ – $J_3$ ) never lost track, always maintaining a minimal error below **0.5%**.
- Computer tests showed that the simulation is very realistic, with a difference of less than **8%** from the theory. When lifting the arm, the welding tool barely drifted off its path (less than **1%** error), confirming the prototype is accurate and reliable.

## 4.2. RECOMMENDATIONS

- Physical implementation of the project is recommended to validate critical real-world constraints, such as variable friction and thermal deformations, thereby evaluating factors that simulation does not fully account for.
- It is suggested that the model be evaluated with new trajectories and geometries to confirm its adaptability, thus ensuring that the prototype responds correctly to cases of work other than those already planned.
- To ensure the quality of the weld on the physical prototype, the use of high-precision gearboxes is recommended in order to avoid mechanical slack and vibrations, which could affect the stability of the arm and the final finish of the weld bead.

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# **APPENDIX A**

## **RESULTS DATA**

TABLE A.1

Simulation results for the Circular (Workspace 1).

AREA DE TRABAJO 1															
SEPARACION DE 3,2 MM POR NORMA (CONTINUO)							SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)								
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	RADIO (mm)	TIEMPO (s) TRAJECTORIA	TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES	NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD (mm/s)	JUNTAS	RADIO (mm)	TIEMPO (s) TRAJECTORIA	TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES
1	8	J1	10	10,42	55,47	99,976	TIENE UN ERROR DEL 2%	1	6	J1	10	10,43	41,43	99,976	TIENE UN ERROR DEL 2%
		J2	240	99,969	260	99,969									
		J3	140	98,706	50	98,706									
		J4	70	99,991	5	98,991									
		J5	7	98,885	5	99,985									
		J6	2	99,616	110	99,616									
2	8	J1	15	11,48	61,48	99,976	TIENE UN ERROR DEL 2%	2	8	J1	15	11,76	52,76	99,975	TIENE UN ERROR DEL 2%
		J2	230	99,966	180	99,966									
		J3	90	99,695	30	99,964									
		J4	42	98,043	5	99,038									
		J5	5	98,151	3	98,029									
		J6	2	99,631	12	99,633									
3	8	J1	20	20,92	61,92	99,977		3	8	J1	20	15,70	56,70	99,978	
		J2	100	99,964	120	99,967									
		J3	30	98,673	30	99,719									
		J4	25	99,228	5	99,166									
		J5	4	98,853	3	99,095									
		J6	2	99,752	12	99,699									
4	8	J1	30	31,40	72,40	99,975		4	8	J1	30	23,55	64,55	99,935	TIENE UN ERROR DEL 2% Y HASTA EL 3%
		J2	102	99,631	120	99,891									
		J3	30	98,659	35	99,331									
		J4	12	99,567	8	98,298									
		J5	3	99,166	2	97,111									
		J6	2	99,815	12	97,127									
5	8	J1	50	52,35	93,35	99,979		5	10	J1	50	30,61	71,61	99,932	TIENE UN ERROR DEL 2%
		J2	100	99,975	100	99,932									
		J3	30	98,308	30	99,575									
		J4	4	99,267	5	99,42									
		J5	3	99,476	1,5	98,498									
		J6	2	99,677	12	98,041									
6	8	J1	70	73,29	114,29	99,977		6	10	J1	70	43,38	84,38	99,983	
		J2	100	98,975	100	99,979									
		J3	30	99,736	30	99,978									
		J4	1,8	99,691	6	99,52									
		J5	2,4	99,66	1,4	99,446									
		J6	2	99,82	12	99,77									
7	8	J1	100	104,71	145,71	99,985		7	10	J1	100	62,42	103,43	99,982	
		J2	100	98,978	100	99,977									
		J3	30	99,772	30	99,778									
		J4	2	99,431	6	99,428									
		J5	3	99,204	1,2	99,683									
		J6	2,5	99,655	12	99,864									
8	8	J1	150	157,07	198,07	99,983		8	12	J1	150	78,31	119,31	99,982	
		J2	120	99,978	100	99,978									
		J3	30	99,826	30	99,835									
		J4	1,8	99,297	5,2	99,413									
		J5	2	99,408	1	99,734									
		J6	2,5	99,781	12	99,895									
9	8	J1	200	209,43	250,43	99,982		9	12	J1	200	104,55	145,55	99,983	
		J2	120	99,975	100	99,975									
		J3	35	99,86	32	99,878									
		J4	1,8	99,424	7	99,417									
		J5	1,6	99,683	1,2	99,591									
		J6	2,5	99,856	12	99,883									
10	8	J1	300	314,15	355,15	99,988		10	12	J1	300	157,07	198,07	99,988	
		J2	140	99,978	100	99,978									
		J3	70	99,925	40	99,925									
		J4	2,5	99,556	6	99,955									
		J5	2	99,489	0,6	99,49									
		J6	2,4	99,848	12	99,872									

TABLE A.2

Simulation results for the Square trajectory (Workspace 1).

AREA DE TRABAJO 1															
SEPARACION DE 3,2 MM POR NORMA (CONTINUO)						SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)									
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	LOGITUD DE LADO (mm)	TIEMPO (s)	TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES	NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD D (mm/s)	JUNTAS	LOGITUD DE LADO (mm)	CUADRADO		OBSERVACIONES	
												TRAYECTORIA	FINAL		TRAYECTORIA
1	8	J1	45	28,52	49,52	99,976	TIENE O PORQUE AL MANDAR LA SEÑAL DA VALORES MUY PEQUEÑOS	1	6	J1	45	28,58	175	49,58	99,975
		J2				110				99,957					
		J3				30				99,747					
		J4				2				0					
		J5				2				97,226					
		J6				2				99,722					
2	8	J1	50	31,86	52,86	99,974	ERROR DEL 5%	2	8	J1	50	23,93	230	44,94	99,976
		J2				120				99,953					
		J3				35				99,713					
		J4				2				0					
		J5				2				95,939					
		J6				3				99,792					
3	8	J1	60	38,52	59,52	99,973	ERROR DEL 4%	3	8	J1	60	28,93	230	49,93	99,977
		J2				120				99,955					
		J3				35				99,748					
		J4				2				0					
		J5				2				96,959					
		J6				3				99,641					
4	8	J1	70	45,19	66,19	99,975	ERROR DEL 2%	4	8	J1	70	33,93	230	54,94	99,968
		J2				130				99,968					
		J3				35				99,716					
		J4				2				99,717					
		J5				2				96,007					
		J6				3				99,694					
5	8	J1	95	61,85	82,85	99,974	ERROR DEL 2%	5	10	J1	95	37,14	300	58,14	99,966
		J2				120				99,967					
		J3				35				99,642					
		J4				2				0					
		J5				2				96,459					
		J6				3				99,721					
6	8	J1	100	65,19	86,19	99,974	ERROR DEL 2%	6	10	J1	100	39,14	300	60,14	99,979
		J2				120				99,965					
		J3				35				99,639					
		J4				2				0					
		J5				2				98,721					
		J6				3				99,791					
7	8	J1	150	98,52	119,52	99,972	ERROR DEL 2%	7	10	J1	150	59,14	300	80,14	99,973
		J2				120				99,97					
		J3				35				99,689					
		J4				3				0					
		J5				2				98,598					
		J6				3				99,842					
8	8	J1	200	131,85	152,85	99,977	ERROR DEL 3%	8	12	J1	200	65,95	340	86,95	99,959
		J2				100				99,968					
		J3				35				99,736					
		J4				3				0					
		J5				2				98,049					
		J6				3				99,843					
9	8	J1	300	198,52	219,52	99,971	ERROR DEL 4%	9	12	J1	300	99,29	340	120,29	99,983
		J2				100				99,965					
		J3				70				99,817					
		J4				3				0					
		J5				2				96,712					
		J6				3				99,684					
10	8	J1	400	265,19	286,19	99,969	ERROR DEL 3%	10	12	J1	400	132,62	340	153,62	99,98
		J2				135				99,975					
		J3				150				99,897					
		J4				3				0					
		J5				6				97,601					
		J6				3				99,609					

TABLE A.3

Simulation results for the Linear trajectory (Workspace 1).

AREA DE TRABAJO 1													
SEPARACION DE 3,2 MM POR NORMA (CONTINUO)						SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)							
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	LÍNEA RECTA EN EL EJE Z		NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD (mm/s)	JUNTAS	LÍNEA RECTA EN EL EJE Z		TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES	
			TAMANO (mm)	TIEMPO (s)				TAMANO (mm)	TIEMPO (s)				
1	8	J1	50	8,33	16,33	1	6	J1	50	6,25	14,25	99,892	ERROR DEL 6%
		J2	325					J2	300		99,891		
		J3	105					J3	98		99,129		
		J4	99,427					J4	4		94,925		
		J5	95,944					J5	6		96,911		
		J6	99,098					J6	1		98,666		
2	8	J1	100	12,50	20,50	2	8	J1	100	10,00	18,00	99,917	
		J2	300					J2	300		99,924		
		J3	95					J3	98		99,429		
		J4	98,571					J4	4		99,131		
		J5	99,677					J5	6		99,556		
		J6	99,686					J6	1		99,344		
3	8	J1	200	25,00	33,00	3	8	J1	200	20,00	28,00	99,953	ERROR DEL 2%
		J2	275					J2	275		99,946		
		J3	85					J3	90		98,929		
		J4	99,202					J4	4		99,132		
		J5	99,773					J5	5		99,689		
		J6	99,398					J6	1		99,568		
4	8	J1	300	37,50	45,50	4	8	J1	300	30,00	36,00	99,954	
		J2	240					J2	300		99,949		
		J3	75					J3	115		99,364		
		J4	99,152					J4	4		99,098		
		J5	99,584					J5	5		99,742		
		J6	99,297					J6	1		99,226		
5	8	J1	400	40,00	48,00	5	10	J1	400	36,36	44,36	99,958	
		J2	340					J2	340		99,955		
		J3	265					J3	115		99,481		
		J4	99,122					J4	4		99,209		
		J5	99,324					J5	5		99,54		
		J6	99,225					J6	1		99,276		
6	8	J1	500	41,66	49,66	6	10	J1	500	45,45	53,45	99,963	
		J2	270					J2	310		99,958		
		J3	90					J3	360		99,958		
		J4	99,226					J4	110		99,522		
		J5	99,557					J5	4		99,076		
		J6	99,192					J6	5		98,992		
7	8	J1	600	50,00	58,00	7	10	J1	600	54,54	62,54	99,965	
		J2	265					J2	230		99,959		
		J3	85					J3	360		99,959		
		J4	99,212					J4	120		99,591		
		J5	99,319					J5	3		99,311		
		J6	99,268					J6	5		99,315		
8	8	J1	700	58,33	66,33	8	12	J1	700	50,00	58,00	99,965	
		J2	230					J2	230		99,965		
		J3	290					J3	360		99,958		
		J4	100					J4	120		99,573		
		J5	99,33					J5	3		99,313		
		J6	99,565					J6	5		99,382		
9	8	J1	800	66,66	74,66	9	12	J1	800	57,14	65,14	99,155	
		J2	190					J2	180		99,965		
		J3	290					J3	350		99,958		
		J4	100					J4	125		99,541		
		J5	99,34					J5	3		99,416		
		J6	99,35					J6	5		99,584		
10	8	J1	900	75	83	10	12	J1	900	64,28	72,28	99,088	
		J2	150					J2	170		99,965		
		J3	270					J3	320		99,957		
		J4	110					J4	125		99,524		
		J5	99,355					J5	3		99,415		
		J6	99,47					J6	5		99,319		

TABLE B.1

Simulation results for the Circular trajectory (Workspace 2).

AREA DE TRABAJO 2																	
SEPARACION DE 3,2 MM POR NORMA (CONTINUO)							SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)										
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	RADIO (mm)	TIEMPO (s) TRAYECTORIA	TIEMPO (s) FINAL	TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES	NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD (mm/s)	JUNTAS	RADIO (mm)	TIEMPO (s) TRAYECTORIA	TIEMPO (s) FINAL	TORQUE MAXIMO (N*m)	ERROR	OBSERVACIONES
1	8	J1	10	10,42	55,47	450	99,976	TIENE UN ERROR DEL 2%	1	6	J1	10	10,43	41,43	260	99,976	TIENE UN ERROR DEL 2%
		J2	240			99,969	320				99,969						
		J3	140			99,706	50				99,706						
		J4	70			98,991	55				98,991						
		J5	7			98,385	5				98,385						
		J6	2			99,616	110				99,616						
2	8	J1	15	11,48	61,48	230	99,976	TIENE UN ERROR DEL 2%	2	8	J1	15	11,76	52,76	180	99,975	TIENE UN ERROR DEL 2%
		J2	155			99,966	120				99,966						
		J3	90			99,695	30				99,964						
		J4	42			98,043	5				99,036						
		J5	5			98,151	3				98,029						
		J6	2			99,631	12				99,623						
3	8	J1	20	20,92	61,92	170	99,977		3	8	J1	20	15,70	56,70	180	99,978	
		J2	100			99,964	120				99,967						
		J3	30			98,673	30				99,719						
		J4	25			99,228	5				99,266						
		J5	4			98,853	3				99,095						
		J6	2			99,752	12				99,699						
4	8	J1	30	31,40	72,40	180	99,975		4	8	J1	30	23,55	64,55	180	99,935	TIENE UN ERROR DEL 2% Y HASTA EL 3%
		J2	102			99,631	120				99,891						
		J3	30			98,659	35				99,331						
		J4	12			99,567	8				98,536						
		J5	3			99,166	2				97,111						
		J6	2			99,815	12				97,427						
5	8	J1	50	52,85	93,35	170	99,979		5	10	J1	50	30,61	71,61	160	99,932	TIENE UN ERROR DEL 2%
		J2	100			99,975	120				99,932						
		J3	30			98,368	30				99,575						
		J4	4			99,267	5				99,42						
		J5	3			99,476	1,5				98,498						
		J6	2			99,677	12				98,041						
6	8	J1	70	73,29	114,29	160	99,977		6	10	J1	70	43,38	84,38	160	99,983	
		J2	100			98,975	120				99,979						
		J3	30			99,736	30				99,78						
		J4	1,8			99,691	6				99,52						
		J5	2,4			99,66	1,4				99,446						
		J6	2			99,82	12				99,77						
7	8	J1	100	104,71	145,71	160	99,985		7	10	J1	100	62,42	103,43	155	99,982	
		J2	100			98,979	120				99,977						
		J3	30			99,772	30				99,778						
		J4	2			99,431	6				99,428						
		J5	3			99,204	1,2				99,683						
		J6	2,5			99,665	12				99,864						
8	8	J1	150	157,07	198,07	180	99,983		8	12	J1	150	78,31	119,31	130	99,982	
		J2	120			98,979	120				99,978						
		J3	30			99,826	30				99,835						
		J4	1,8			99,297	5,2				99,413						
		J5	2			99,408	1				99,734						
		J6	2,5			99,781	12				99,895						
9	8	J1	200	209,43	250,43	180	99,982		9	12	J1	200	104,55	145,55	120	99,983	
		J2	120			99,975	120				99,978						
		J3	35			99,86	32				99,878						
		J4	1,8			99,424	7				99,417						
		J5	1,6			99,683	1,2				99,591						
		J6	2,5			99,856	12				99,883						
10	8	J1	300	314,15	355,15	165	99,988		10	12	J1	300	157,07	198,07	85	99,988	
		J2	140			99,978	85				99,978						
		J3	70			99,975	40				99,925						
		J4	2,5			99,556	6				99,955						
		J5	2			99,489	0,6				99,49						
		J6	2,4			99,849	12				99,872						

TABLE B.2

Simulation results for the Square trajectory (Workspace 2).

AREA DE TRABAJO 2																	
SEPARACION DE 3,2 MM POR NORMA (CONTINUO)					SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)												
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	LOGITUD DE LADO (mm)	TIEMPO DE TRAYECTORIA	CUADRADO		OBSERVACIONES	NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD D (mm/s)	JUNTAS	LOGITUD DE LADO (mm)	TIEMPO DE TRAYECTORIA	TIEMPO (s)	CUADRADO		OBSERVACIONES	
					TORQUE MAXIMO (N*m)	ERROR								TORQUE MAXIMO (N*m)	ERROR		
1	8	J1	45	28,52	49,52	175	99,576	TIENE O PORQUE AL MANDAR LA SEÑAL DA VALORES MUY PEQUEÑOS	1	6	J1	45	28,58	49,58	175	99,575	ERROR DEL 3%
		J2				110	99,557				110				99,557		
		J3				30	99,747				35				99,747		
		J4				2	0				2				0		
		J5				2	97,236				2				97,146		
		J6				2	99,722				1				99,722		
2	8	J1	50	31,86	52,86	120	99,974	ERROR DEL 5%	2	8	J1	50	23,93	44,94	230	99,976	ERROR DEL 3%
		J2				120	99,953				115				99,965		
		J3				35	99,713				35				99,747		
		J4				2	0				2				0		
		J5				2	95,939				2				97,963		
		J6				3	99,752				1				99,754		
3	8	J1	60	38,52	59,52	230	99,973	ERROR DEL 4%	3	8	J1	60	28,93	49,93	230	99,977	ERROR DEL 2%
		J2				120	99,958				115				99,968		
		J3				35	99,748				35				99,682		
		J4				2	0				2				0		
		J5				2	96,959				2				96,968		
		J6				3	99,641				1				99,852		
4	8	J1	70	45,19	66,19	180	99,975	ERROR DEL 2%	4	8	J1	70	33,93	54,94	230	99,968	ERROR DEL 2%
		J2				120	99,967				115				99,968		
		J3				35	99,716				35				99,717		
		J4				2	0				2				0		
		J5				2	96,007				2				96,739		
		J6				3	99,694				1				99,883		
5	8	J1	95	61,85	82,85	240	99,974	ERROR DEL 2%	5	10	J1	95	37,14	58,14	300	99,966	ERROR DEL 2%
		J2				120	99,965				110				99,967		
		J3				35	99,639				35				99,71		
		J4				2	0				3				0		
		J5				2	98,459				2				98,715		
		J6				3	99,721				2				99,88		
6	8	J1	100	65,19	86,19	240	99,974	ERROR DEL 2%	6	10	J1	100	39,14	60,14	300	99,979	ERROR DEL 2%
		J2				120	99,965				110				99,972		
		J3				35	99,639				35				99,703		
		J4				2	0				3				0		
		J5				2	98,721				2				98,67		
		J6				3	99,791				2				99,884		
7	8	J1	150	98,52	119,52	240	99,972	ERROR DEL 2%	7	10	J1	150	59,14	80,14	300	99,972	ERROR DEL 2%
		J2				120	99,957				110				99,967		
		J3				35	99,689				35				99,742		
		J4				3	0				3				0		
		J5				2	96,598				2				96,794		
		J6				3	99,842				2				99,852		
8	8	J1	200	131,85	152,85	300	99,977		8	12	J1	200	65,95	86,95	340	99,959	ERROR DEL 3%
		J2				100	99,968				100				99,962		
		J3				35	99,756				75				99,766		
		J4				3	0				3				0		
		J5				2	99,049				2				97,945		
		J6				3	99,843				2				99,796		
9	8	J1	300	198,52	219,52	270	99,971	ERROR DEL 4%	9	12	J1	300	99,29	120,29	340	99,983	
		J2				100	99,965				100				99,964		
		J3				70	99,817				75				99,812		
		J4				3	0				3				0		
		J5				2	96,712				2				99,245		
		J6				3	99,654				2				99,886		
10	8	J1	400	265,19	286,19	260	99,969	ERROR DEL 3%	10	12	J1	400	132,62	159,62	340	99,98	ERROR DEL 2%
		J2				135	99,975				100				99,96		
		J3				150	99,897				75				99,856		
		J4				3	0				3				0		
		J5				6	97,601				2				98,76		
		J6				3	99,609				2				99,868		

TABLE B.3

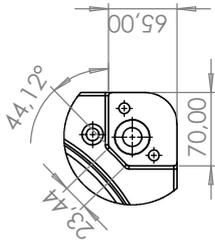
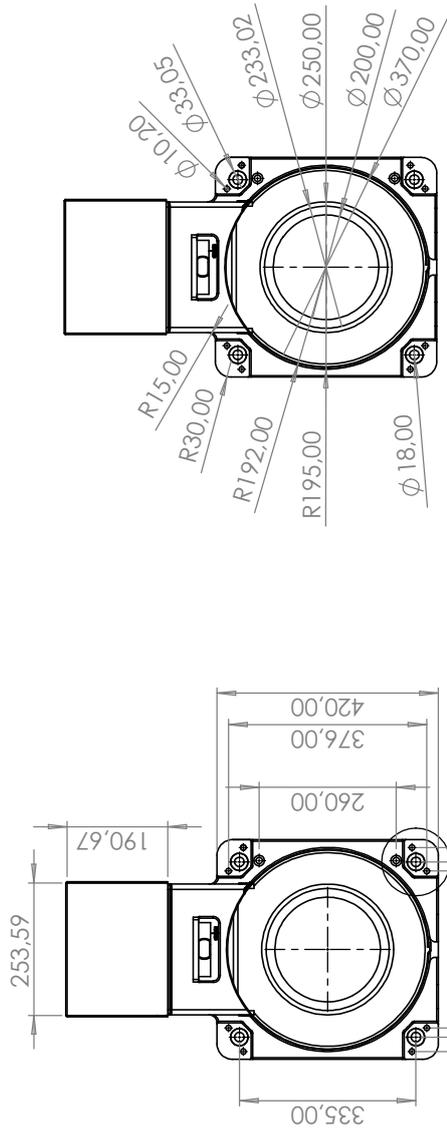
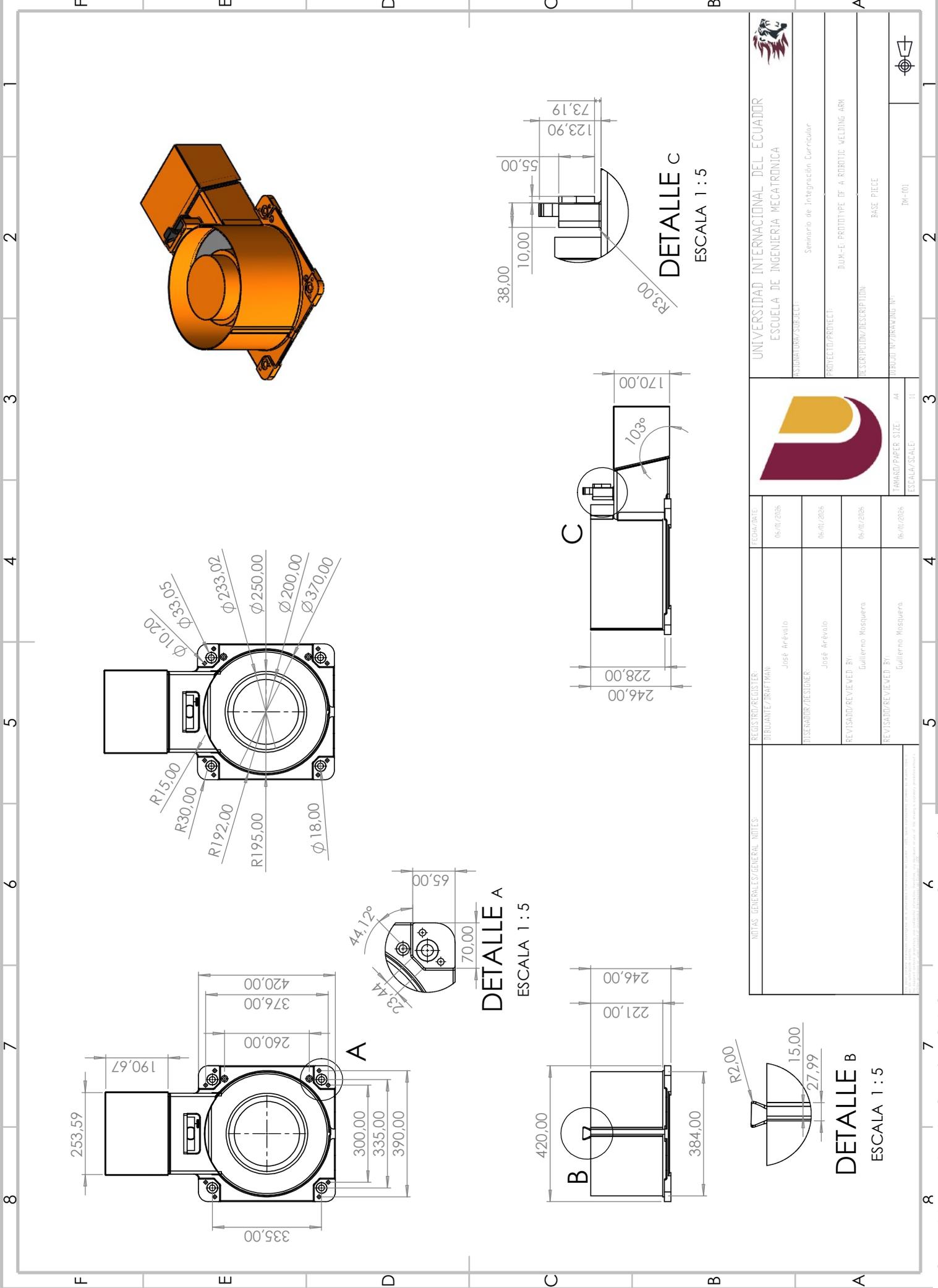
Simulation results for the Linear trajectory (Workspace 2).

AREA DE TRABAJO 2														
SEPARACION DE 3,2 MM POR NORMA (SIN INTERMITENCIA)							SEPARACION DE 40 MM POR NORMA (CON INTERMITENCIA)							
NUMERO DE PRUEBA CONTINUO	VELOCIDAD (mm/s)	JUNTAS	LINEA RECTA EN EL EJE Z			NUMERO DE PRUEBA INTERMITENTE	VELOCIDAD (mm/s)	JUNTAS	LINEA RECTA EN EL EJE Z			ERROR	OBSERVACIONES	
			TAMANO (mm)	TIEMPO (s)	TORQUE MAXIMO (N*m)				TAMANO (mm)	TIEMPO (s)	TORQUE MAXIMO (N*m)			
1	8	J1	50	8,33	16,33	1	6	J1	50	6,25	14,25	400	J1	99,894
		J2	325	99,909	J2			300	99,891					
		J3	105	99,427	J3			98	99,129					
		J4	4	95,944	J4			4	94,525					
		J5	5	99,098	J5			6	98,511					
		J6	1	99,007	J6			1	98,666					
2	8	J1	100	12,50	20,50	2	8	J1	100	10,00	18,00	300	J1	99,517
		J2	300	99,936	J2			300	99,924					
		J3	95	99,09	J3			98	99,429					
		J4	4	98,571	J4			4	99,131					
		J5	5	99,677	J5			6	99,556					
		J6	1	99,636	J6			1	99,344					
3	8	J1	200	25,00	33,00	3	8	J1	200	20,00	28,00	380	J1	99,533
		J2	275	99,95	J2			275	99,946					
		J3	85	99,205	J3			90	98,979					
		J4	3	99,202	J4			4	99,132					
		J5	5	99,73	J5			5	99,689					
		J6	1	99,398	J6			1	99,568					
4	8	J1	300	37,50	45,50	4	8	J1	300	30,00	38,00	365	J1	99,554
		J2	240	99,956	J2			300	99,949					
		J3	75	99,389	J3			115	99,364					
		J4	4	99,152	J4			4	99,098					
		J5	5	99,584	J5			5	99,742					
		J6	1	99,297	J6			1	99,276					
5	8	J1	400	40,00	48,00	5	10	J1	400	36,36	44,36	340	J1	99,566
		J2	265	99,961	J2			340	99,953					
		J3	90	99,58	J3			115	99,481					
		J4	3	99,122	J4			4	99,09					
		J5	5	99,324	J5			5	99,54					
		J6	1	99,225	J6			1	99,276					
6	8	J1	500	41,66	49,66	6	10	J1	500	45,45	53,45	310	J1	99,965
		J2	270	99,96	J2			360	99,958					
		J3	90	99,55	J3			110	99,522					
		J4	3	99,26	J4			4	99,078					
		J5	4	99,557	J5			5	98,932					
		J6	1	99,192	J6			1	99,219					
7	8	J1	600	50,00	58,00	7	10	J1	600	54,54	62,54	230	J1	99,965
		J2	265	99,96	J2			360	99,959					
		J3	85	99,589	J3			120	99,991					
		J4	3	99,212	J4			3	99,311					
		J5	3	99,319	J5			5	99,315					
		J6	1	99,208	J6			1	99,188					
8	8	J1	700	58,33	66,33	8	12	J1	700	50,00	58,00	230	J1	99,965
		J2	290	99,959	J2			360	99,958					
		J3	100	99,542	J3			120	99,973					
		J4	2	99,33	J4			3	99,313					
		J5	4	99,565	J5			5	99,382					
		J6	1	99,137	J6			1	99,155					
9	8	J1	800	66,66	74,66	9	12	J1	800	57,14	65,14	180	J1	99,969
		J2	290	99,962	J2			350	99,958					
		J3	100	99,535	J3			125	99,541					
		J4	2	99,34	J4			3	99,416					
		J5	4	99,35	J5			5	99,584					
		J6	1	99,143	J6			1	99,088					
10	8	J1	900	75	83	10	12	J1	900	64,28	72,28	170	J1	99,969
		J2	270	99,96	J2			320	99,957					
		J3	110	99,526	J3			125	99,524					
		J4	2	99,35	J4			3	99,415					
		J5	4	99,47	J5			5	99,319					
		J6	1	99,055	J6			1	99,038					

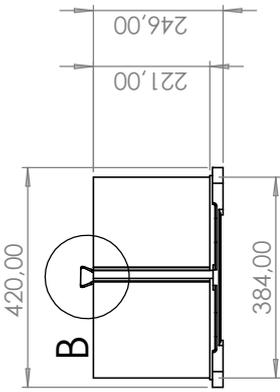
# **APPENDIX B**

## **D.U.M.-E ROBOTIC ARM PLANS**

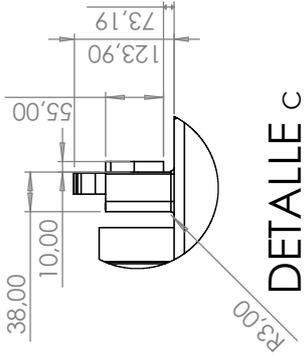
*D.U.M.E. (Digital Unit for MIG Experimentation)*



**DETALLE A**  
ESCALA 1 : 5



**DETALLE B**  
ESCALA 1 : 5



**DETALLE C**  
ESCALA 1 : 5



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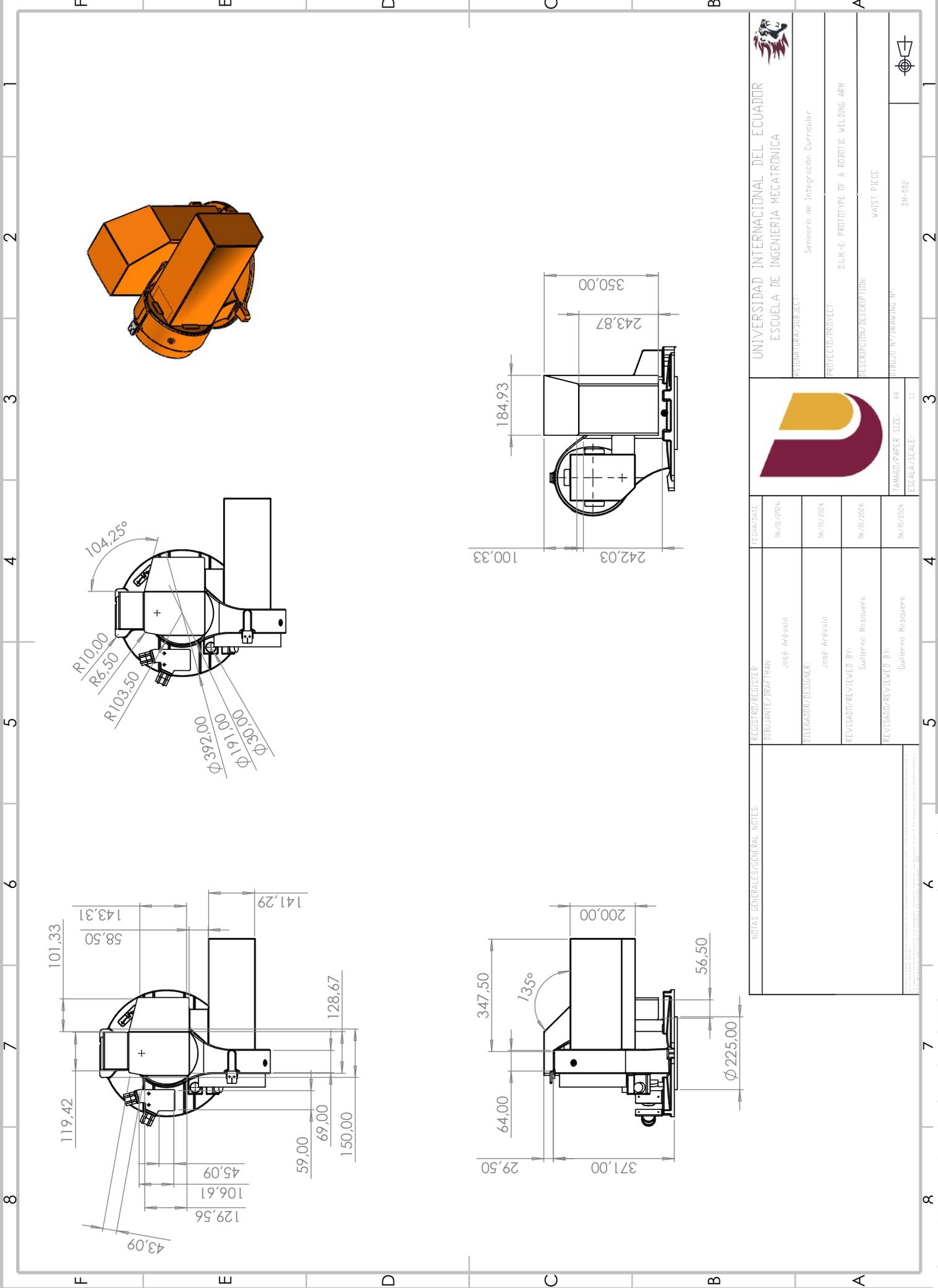
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PROYECTO/PROJECT: DUM-E-PROTOTYPE OF A ROBOTIC WELDING ARM

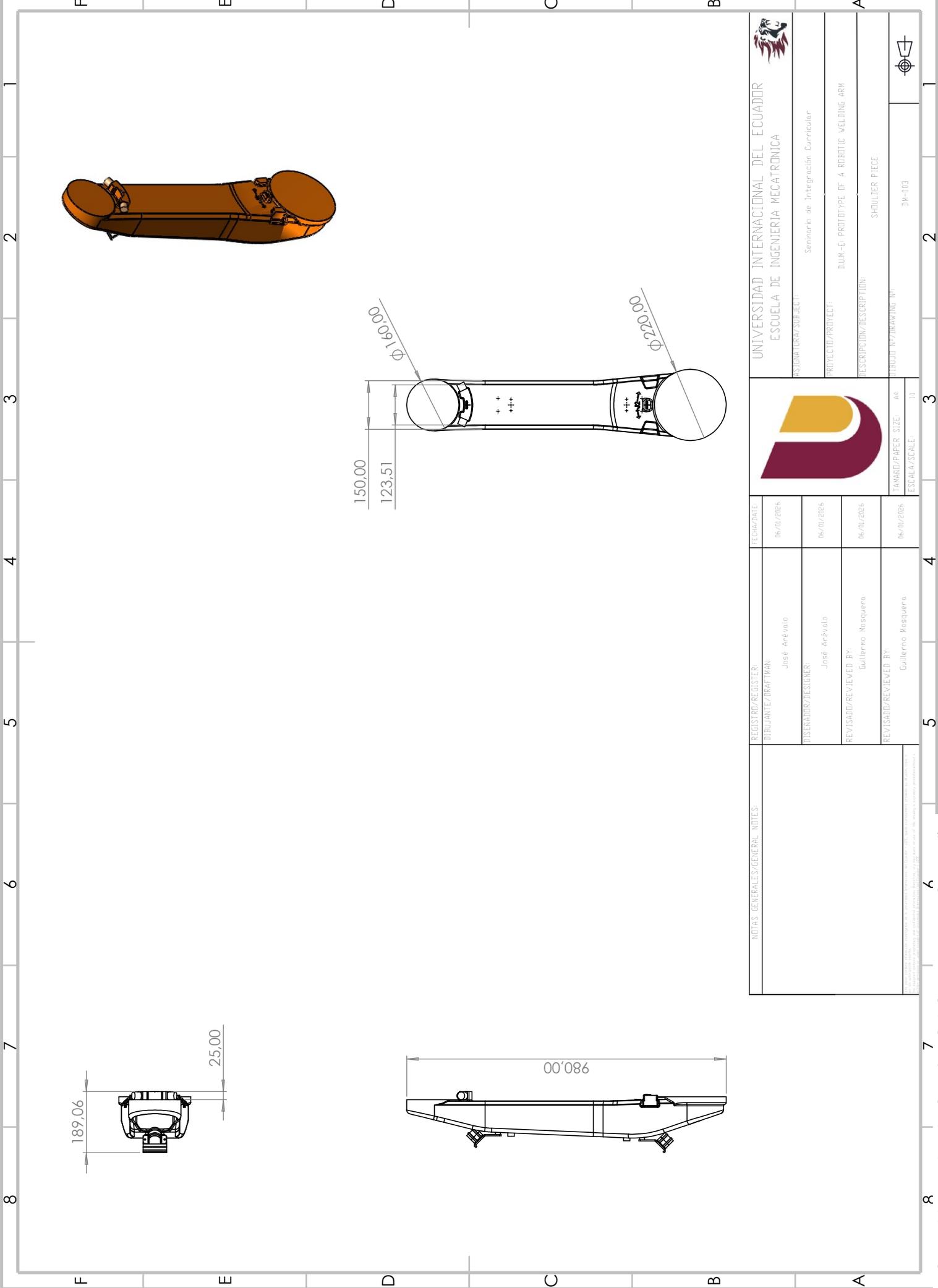
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TABLON/WORKING N°: JM-001

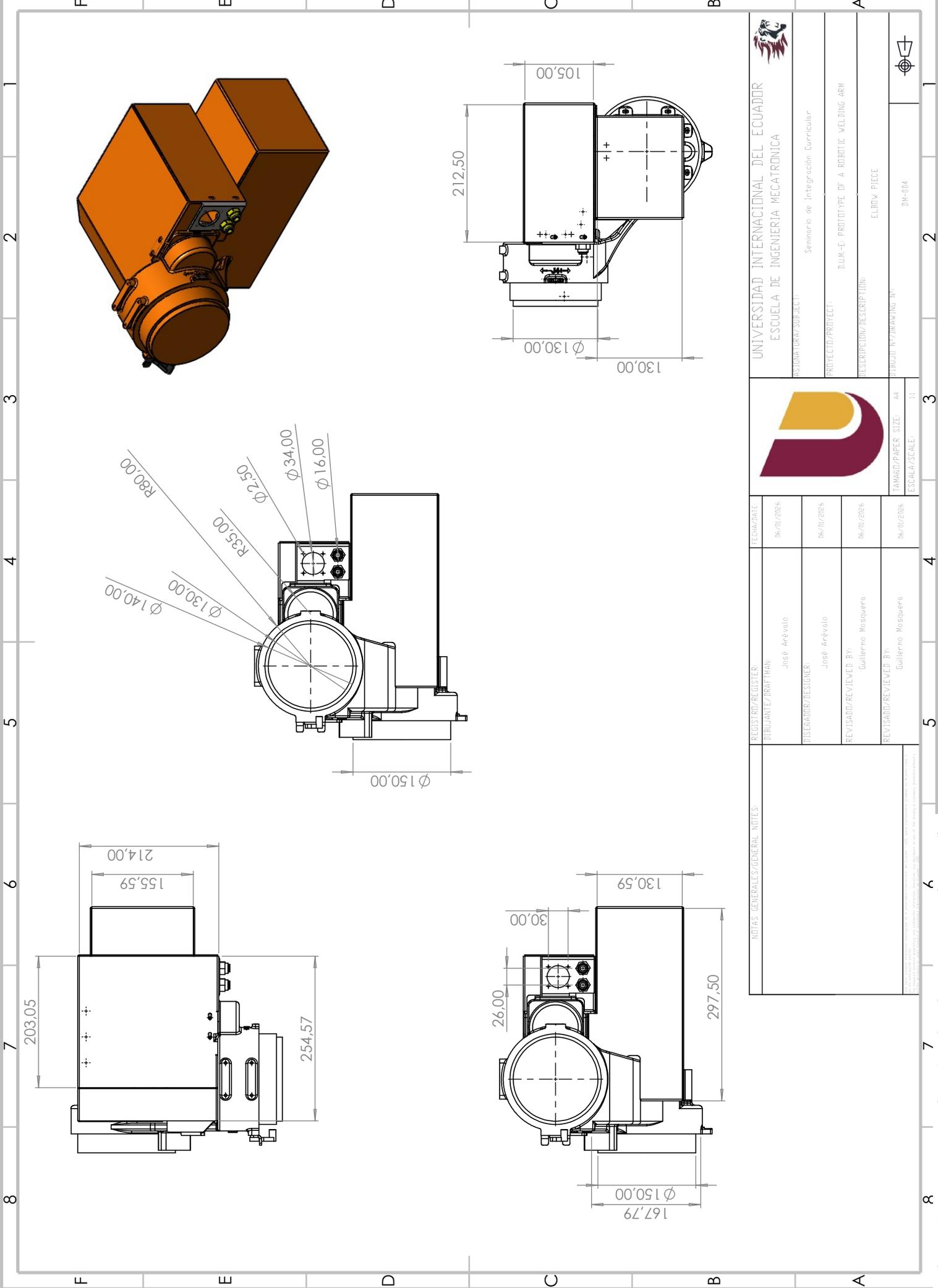
REGISTRO/REGISTER:	ESCALA/SCALE:
DIBUJANTE/DRAWING: JOSE ARVELO	06/01/2026
DISEÑADOR/DESIGNER: JOSE ARVELO	06/01/2026
REVISADO/REVIEWED BY: GUILLERMO MASQUERA	06/01/2026
REVISADO/REVIEWED BY: GUILLERMO MASQUERA	06/01/2026



 UNIVERSIDAD INTERNACIONAL DEL ECUADOR ESCUELA DE INGENIERIA MECATRONICA	HISTORIADOR/SUBJECT: Seminario de Integración Curricular	ESCHE/DATE: 06/07/2016	 TAMAÑO/PAPER SIZE: A4 ESCALA/SCALE: 1:1
	PROYECTO/PROJECT: D.U.M.-E. PROTOTYPE OF A ROBOTIC WELDING ARM	DISEÑADOR/DRAWER: José Arévalo	
	DESCRIPCIÓN/DESCRIPTION: WAIST PIECE	REVISADO/REVIEWED BY: Guillermo Mosquera	
	TÍTULO/TITLE: D.U.M.-E. PROTOTYPE OF A ROBOTIC WELDING ARM	REVISADO/REVIEWED BY: Guillermo Mosquera	



NOTAS GENERALES/GENERAL NOTES:	REGISTRADO/REGISTER:	FECHA/DATE:		UNIVERSIDAD INTERNACIONAL DEL ECUADOR ESCUELA DE INGENIERIA MECATRONICA 	
	DISEÑADOR/DRAWER:	06/07/2016			SEMESTRE DE INTEGRACIÓN CURRICULAR
	REVISADO/REVIEWED BY:	06/07/2016			DISEÑO DE PROTOTIPO DE A ROBOTIC WELDING ARM
	REVISADO/REVIEWED BY:	06/07/2016			DESCRIPCIÓN/DESCRIPTION: SHOULDER PIECE
		06/07/2016	TAMAÑO/PAPER SIZE: A4	IDENTIFICACION/IDENTIFICATION: DM-003	
			ESCALA/SCALE: 1:1		



UNIVERSIDAD INTERNACIONAL DEL ECUADOR  
 ESCUELA DE INGENIERIA MECATRONICA

ASTUTORIA/SUBJECT: Seminario de Integración Curricular

PROJECT/PROJECT: DUM-E- PROTOTYPE OF A ROBOTIC WELDING ARM

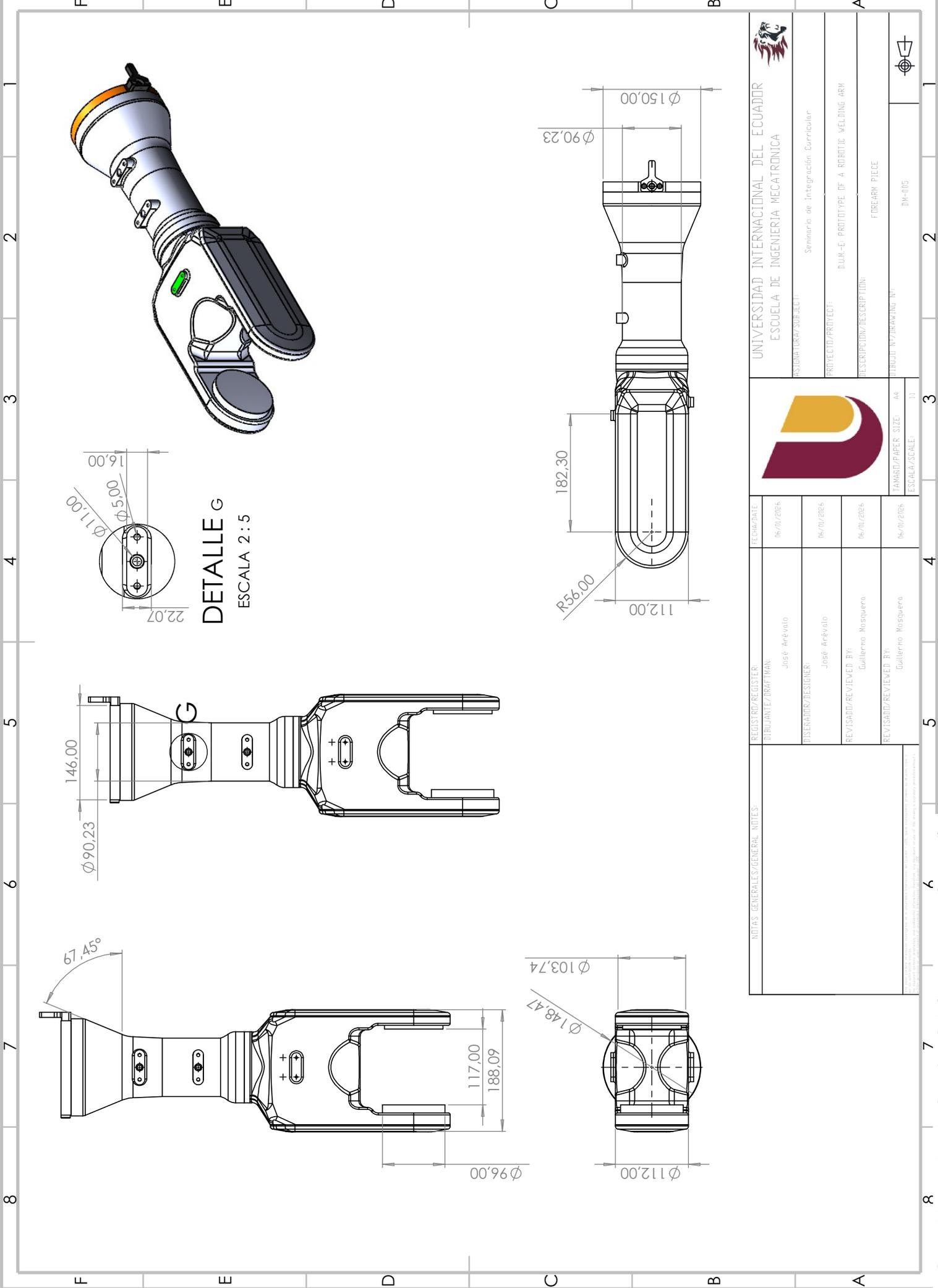
DESIGNER/DESIGNER: ELBOV- PIERCE

TUTOR/ TUTORING N°: DM-004



REGISTRADO/REGISTER	FECHA/DATE
DISEÑADOR/DRAWER: José Arévalo	06/07/2016
REVISADO/REVIEWER: José Arévalo	06/07/2016
REVISADO/REVIEWER BY: Guillermo Mosquera	06/07/2016
REVISADO/REVIEWER BY: Guillermo Mosquera	06/07/2016

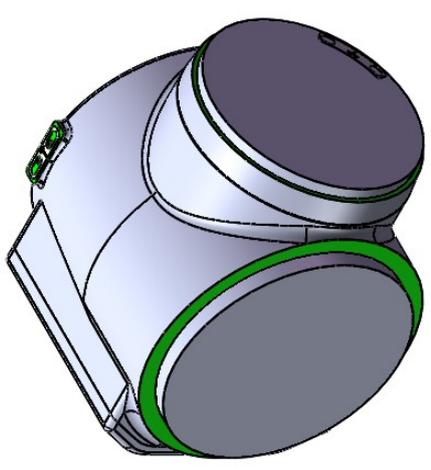
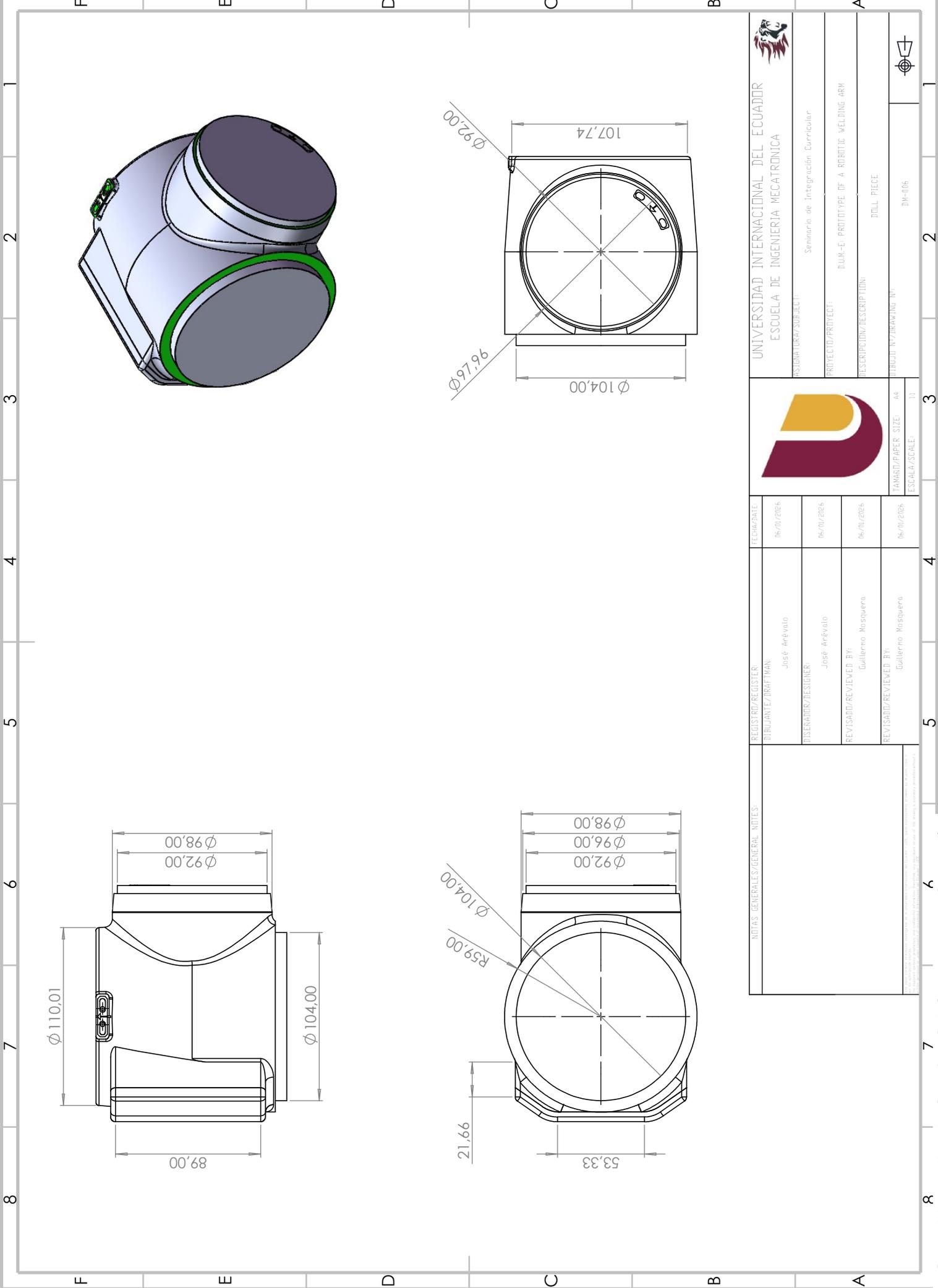
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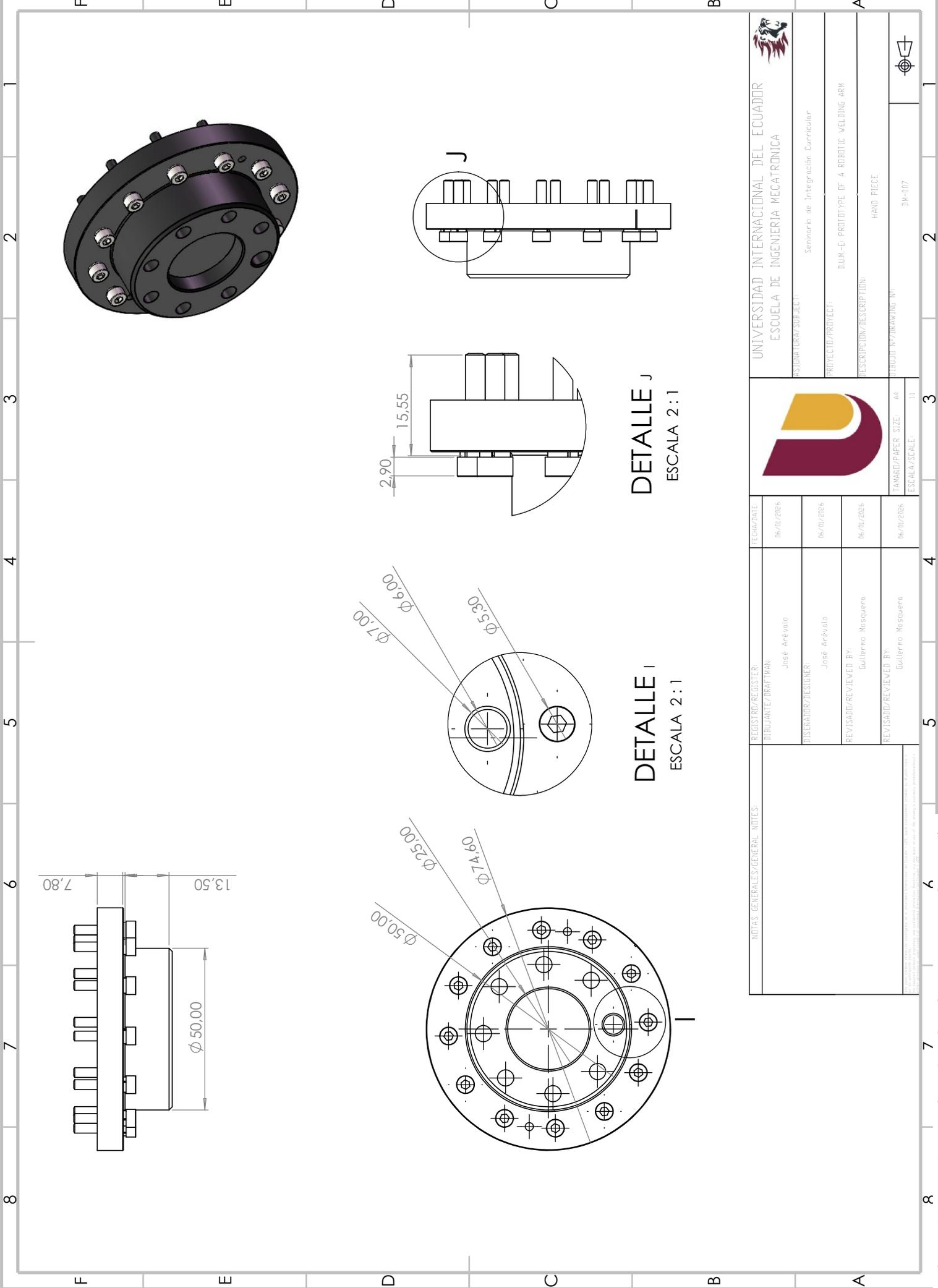
 UNIVERSIDAD INTERNACIONAL DEL ECUADOR ESUELA DE INGENIERIA MECATRONICA		Seminario de Integración Curricular DUM-E- PROTOTYPE OF A ROBOTIC WELDING ARM FOREARM-PIECE	
ASISTENTE/SUBJECT:		TUBO/PIPE/DRAWING: N°	
PROYECTO/PROJECT:		TAMANO/PAPER SIZE: A4	
DESCRIPCIÓN/DESCRIPTION:		ESCALA/SCALE: 1:1	

	FECHA/DATE: 06/07/2016
	REGISTRO/REGISTER: DISEÑADOR/DRAWER: José Arévalo
	REVISADO/REVIEWED BY: Guillermo Mosquera
	REVISADO/REVIEWED BY: Guillermo Mosquera

NOTAS- GENERALES/GENERAL NOTES:	REGISTRO/REGISTER: DISEÑADOR/DRAWER: José Arévalo	FECHA/DATE: 06/07/2016
REVISADO/REVIEWED BY: Guillermo Mosquera	REVISADO/REVIEWED BY: Guillermo Mosquera	TAMANO/PAPER SIZE: A4
REVISADO/REVIEWED BY: Guillermo Mosquera	REVISADO/REVIEWED BY: Guillermo Mosquera	ESCALA/SCALE: 1:1



NOTAS GENERALES/GENERAL NOTES:	REGISTRADO/REGISTER:	FECHA/DATE:	 UNIVERSIDAD INTERNACIONAL DEL ECUADOR ESCUELA DE INGENIERIA MECATRONICA	 Seminario de Integración Curricular DUM-E PROTOTYPE OF A ROBOTIC WELDING ARM DISEÑO/DESIGN: DIM-006	
	DISEÑADOR/DRAWER:	06/07/2016			PROYECTO/PROJECT:
	REVISADO/REVIEWED BY:	06/07/2016			DESCRIPCIÓN/DESCRIPTION:
	REVISADO/REVIEWED BY:	06/07/2016			TÍTULO/TITLE:
		06/07/2016	TAMANO/PAPER SIZE: A4	DM-006	
		06/07/2016	ESCALA/SCALE: 1:1		



**DETALLE J**  
ESCALA 2:1

**DETALLE I**  
ESCALA 2:1

 UNIVERSIDAD INTERNACIONAL DEL ECUADOR ESCUELA DE INGENIERIA MECATRONICA	HISTORIA/PROYECTO: Seminario de Integración Curricular	FECHA/DATE: 06/07/2016	 TAMAÑO/PAPER SIZE: A4 ESCALA/SCALE: 1:1
	PROYECTO/PROJECT: D.U.M.-E. PROTOTYPE OF A ROBOTIC WELDING ARM	DISEÑADOR/DRAWER: José Arévalo	
	DESCRIPCIÓN/DESCRIPTION: HAND PIECE	REVISADO/REVIEWED BY: Guillermo Masquera	
	TÍTULO/TITLE: DM-007	REVISADO/REVIEWED BY: Guillermo Masquera	